



# **An effective Decision making model through Fusion Optimization and risk associated with flash flood hazards: A case study Asyut, Egypt**

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## **Abstract**

One of the most dangerous natural disasters, which causes massive damage all over the world, is flash floods. Therefore, the assessment of flash floods disasters is considered increasingly urgent and important. The widely used techniques for studying and analyzing the causes and impact of natural hazards are multi-criteria techniques. Several researchers used traditional multi-criteria decision-making techniques in the estimation process of flash floods problems as the analytical hierarchy process, decision making trial and evaluation laboratory and analytic network process. The main disadvantage of these traditional models is the incapability of simulating and reflecting uncertain human thoughts. Since neutrosophic logic has a great ability for simulating human's thoughts and increase the flexibility of expert's preferences in real world problems, we applied it in this study. There are different locations in Egypt that are at a serious risk of flooding, especially in Upper Egypt. Asyut has suffered from frequent flash floods, with some flood events that lead to mortality, damages, and economic losses in the last decades. The intensity of floods in Egypt varies from year to year, according to several climatic and hydrological variables. This study focuses on using a Neutrosophic Decision making trial and evaluation laboratory (N-DEMATEL) technique with remotely sensed data and geographical information system (GIS) for producing a flash floods hazard map. The N-DEMATEL technique is applied to determine the weights of various factors that related to flash flooding, including elevation, slope, topographic wetness index, distance from the stream, flow accumulation, aspect, flow direction, soil, land cover, watershed, curvature, drainage density, total population, population density and precipitation. The obtained weight of selected criteria used then to produce the flood hazard map (FHM) using a raster calculator tool in geographic information system.

**Keywords:** Neutrosophic Set; Multi-Criteria Decision-Making Technique (MCDM); Decision making trial and evaluation laboratory (DEMATEL); Geographic Information System (GIS); Flood Hazard Map.

## **1. Introduction**

As we know, flash floods are considered as one of the most natural disasters which cause massive damage all over the world. In recent decades, flash flood hazards have increased all over the world. Flash flood is caused by severe rainfall on specific area over a short time [1, 2]. Due to climate change, the world is facing increasingly frequent and heavy rainfall [3]. Continuous increases in the concentration of greenhouse gases will cause further global climate change. Climate change is projected to change the floods frequency, magnitude, and severity [4]. Many studies show the effect of climate change on the occurrence of extreme regional phenomena of precipitation and focus on the resulting changes in the volume of precipitation and the occurrence of floods [5]. So, the assessment of flash flood disasters is considered

increasingly urgent and important. In recent years, flash flood hazard maps are a very important component to reduce risk of flash floods.

Flash flood risk maps provide residents with information about potential damage and how to prevent probable disasters. These maps are produced in many forms, such as maps for emergency plans, flood tracking, flood hazard reduction and flood information, as well as for many other purposes [6]. Recently, integrating GIS and remote sensing (RS) has been used to produce risk maps. There are many factors that used for producing flash flood susceptibility maps and depends on the effect and importance of each independent factor and varies between different areas, including elevation, slope, topographic wetness index, distance from the stream, flow accumulation, aspect, and flow direction, soil, land cover, watershed, curvature, total population , population density and precipitation [3, 7-9].

There are various locations in Egypt that were subjected to flash floods, which caused human losses and damage to infrastructure [1,2]. Upper Egypt is considered one of the most vulnerable places to floods [10-12] and described in Table1.

Multi-criteria decision-making analysis is a broad term that used to describe several models that facilitate decision making and considering many criteria within a defined system. Several studies have used various multi-criteria decision-making techniques and combined it with remotely sensed data and geographical information system (GIS) for producing a flash flood hazard map. Many authors applied different multi criteria models to assign an optimal criterion weight according to their relative importance Some of the MCDM approaches such as ANP, AHP and TOPSIS have been united with geographical information system and remotely sensed data at flash flood susceptibility assessment [2,9,13-19].

In literature there does not exist any model which combined neutrosophic DEMATEL technique with GIS for analyzing flash floods problems. DEMATEL was first developed by the Science and Human affairs Program of the Battelle Memorial Institute of Geneva [20]. DEMATEL is an effective way to identify the components of the cause chain in a complex system [21]. It deals with evaluating interdependent relationships among factors and finding the critical ones through a visual structural model. Due to its capabilities and advantages, the DEMATEL approach has received a lot of attention in the past decade and many researchers have applied it to solve complex system problems in many fields.

Our study focuses on extending the DEMATEL technique under neutrosophic environment and combining it with remotely sensed data and geographical information system (GIS) for producing a flash flood hazard map.

Table 1: Historical flash floods events in Egypt

<b>Flash flood location</b>	<b>Date</b>	<b>Type of damage</b>
Giza	1972	180 destroyed houses, 1500 people affected, roads cutoff, and inundation of agricultural areas
Wad El-Arish, Sinai	February 1975	280 destroyed houses, 17 deaths, and thousands became homeless
Sohag, Asyut, and Kom-Ombo in Aswan	May, 1979	200 houses demolished, 3 deaths, 10,000 acres of farmland were flooded
Asyut, Sohag, and Idfu	October, 1979	1576 destroyed houses and 8841 homeless
Kom-Ombo, Aswan	October, 1979	Destruction of nearly three hundred houses
Wadi Watir, Sinai	October, 1987	27 persons were injured, many deaths, highways damages
Wadi Sudr	January, 1988	5 loss of life
Wadi Dahab, Sinai	September, 1994	40% of the highway of Nuweiba City were destroyed
Asyut	November, 1994	Explosion of oil tanks, deaths, various damages, and economic losses in Drunka village
Sinai, Red Sea, and Aswan	January, 2010	Awan: 500 families became homeless, North Sinai: 6 deaths and hundreds were injured, South Sinai: 2 deaths and 16 were injured
Wadi Dahab and Catherine, Sinai	October, 2012	Power were cutoff, and houses were destroyed
South Sinai	January, 2013	2 deaths, 19 injury, Nuweiba roads were partially destroyed and cutoff telecommunication network

Qena	January, 2013	Deaths and various damages
Asyut	March, 2014	Dam failure
Sinai and Red Sea	March, 2014	Various damages, destruction events, people deaths, and injuries
Taba, South Sinai	May, 2014	1 death, 7 injures, 70 family were displaced and severe economic losses
Sohag	October, 2016	Partial failure in Sohag Dam
Asyut	November, 2018	Partial failure in Asyut Dam

The structure of this research is planned as follow: Section 2 describes the study area and flash flood influencing factors with details. Section 3 describes some basics of neutrosophic theory. Section 4 describes the proposed method of neutrosophic DEMATEL based GIS. The application of the proposed method is described in section 5. Section 6 describes results and discussions of study area using proposed method. Section 7 summarizes research and conclusions of this study.

**2.STUDY AREA AND FLASH FLOOD INFLUENCING FACTORS**

Asyut is situated in Upper Egypt and is located between latitudes 26° 45' to 27° 30' N and longitudes 30° 30' to 31° 30' E as seen in Figure .1 . The study area covers approximately 16,485 km2; the city lies 400 km south of Cairo. Asyut governorate is divided by the river Nile into two sections, western and eastern. Rainfall in the Asyut region is very variable and can happen at high rates and unexpectedly. Susceptibility to floods increases when the rate of rainfall is higher than the ability of the soil to absorb water and is higher than the rate of water evaporation. [3] mentioned in his research that Asyut is an arid area with a desert climate characterized by hot dry summer with a 37.4 °C average monthly temperature during June and a high evaporation rate (average 14.2 mm/day). The total population in Asyut about 4,431,750 million and population density is 330 people per km2. According to the Egyptian Meteorological Authority (EMA) the annual precipitation average in winter reaches 7 mm. Asyut was subjected to heavy rains (96 mm) from the 15th to the 18th of November, 2018 which led to devastating floods [3].

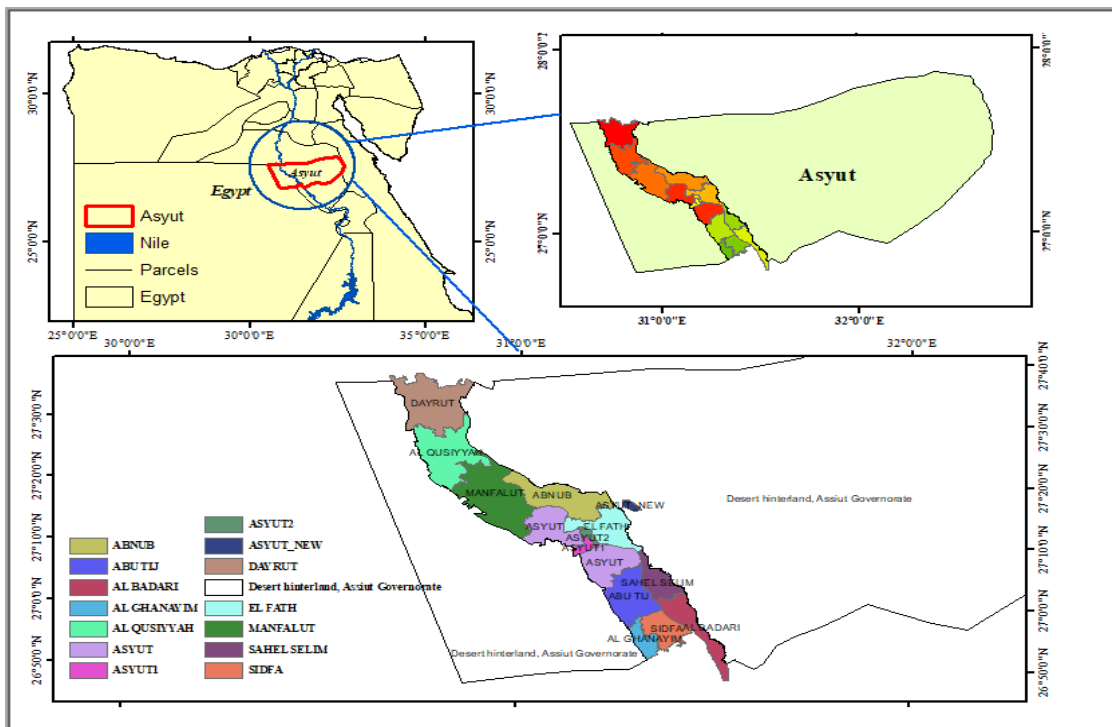


Figure 1: Asyut governorate in Egypt

The focus of flood hazard mapping and susceptibility mapping is to determine influencing factors. The determination process of factors, which causes flooding, is mostly based on previous studies and expert opinion in the field. The choice of spatial reference criteria or factors is very important step in decision-making analysis. [22] used the following influencing factors: slope, elevation, distance from stream, and hydrologic units. While [23] assumed factors as follows: slope, cover type, elevation, land use, population density and distance from river and mainstream. Also, [24] used lithology, slope, drainage network, wetness index of topographic, elevation and curvature as influencing factors. As said by [25], geological, hydrogeological, and physio-geographical factors that affect flash floods include slope, soil type, precipitation, catchment area and land use. Also [9] used the following six flood causative factors: digital elevation model (DEM), slope, distance from stream, topographic wetness index (TWI), lithological units, and land use (LULC). Both elevation and slope have the highest values in terms of susceptibility of flooding, while the area of low slopes and low ground elevation are more susceptible to flash floods [24].

From reviewing relevant literature, we selected elevation, slope, topographic wetness index, distance from the stream, flow accumulation, aspect, flow direction, soil, land cover, watershed, curvature, drainage density, total population, population density and precipitation as the main flash flood factors for our study as follows:

### **2.1 Elevation**

Shuttle Radar Topography Mission (SRTM) data with 30 m spatial resolution were acquired from the United State Geological Survey (USGS) <http://gdex.cr.usgs.gov/gdex>. (SRTM) data are used for extracting the digital elevation model DEM as seen in Figure .2. The low altitude lands are more prone to flooding, whilst higher land is less prone to flooding. According to [26] areas of lower elevation are more prone to flooding as water is flow into the lowlands more than the highlands. Accordingly, “lower elevation” as a factor increases flood susceptibility.

### **2.2 Slope**

Slope is a measure of the degree of inclination or steepness and is one of the greatest floods influencing factors because it determines the water velocity. Slope is an important in determining risk of flash floods for the reason of its influence on stream water flows and runoff. Areas with gentle slopes are more prone to flooding, as low-lying and sloping areas are the first to be submerged when a flood enters an area. The slope of our study area seen in Figure .3. The low slope degree given the highest rating.

### **2.3 Topographic Wetness Index (TWI)**

TWI is an indicator that determines the ability of the Earth’s surface to be saturated with water and could determine overland flow output. TWI pointing to the propensity for flow accumulation determines the influence of topography on hydrological processes, and it is a useful indicator for assessing flood vulnerability [27]. Many researchers have used TWI as an input to develop predictive maps regarding hazard risk of wildfire landslide susceptibility and soil sensitivity. The TWI shown in Figure .4

### **2.4 Aspect**

Aspect is the direction of slope. Aspect has a role on the runoff of surface due to its impact on the other factors like solar radiation, rainfall regime and soil humidity. Aspect starts at the north with 0°, ends at the north with 360° moves and move clockwise. An aspect of 10° is closer than 30° to 360° as it is a circular measure. We must manipulate measures of aspect before using them in data analysis. In our study shown in Figure .5.

### **2.5 Soil and Land use land cover (LULC)**

A soil property, ST describes the relative proportion of different grain sizes of mineral particles in a soil and determines the water infiltration and runoff generation. Soil structure size ranges from fine to medium particle [28]. LULC describes the appearance of the landscape. Soil and LULC data were acquired from food and agriculture organization of the United Nations (FAO). Soil raster and LULC raster are both shown in Figure .6 and Figure .7.

### **2.6 Precipitation**

Precipitation data during the time period 2011-2020, are downloaded for free from <https://crudata.uea.ac.uk/cru/data/hrg/>. The analysis of data includes four stages. The images are downloaded in .tif

format with GCS projection, then convert the images to Arc-GIS format. The next step is to clip the images to match the study area. The images are converted to points and resampled into 30 m spatial resolution images. The final stage is to estimate the precipitation in no-data areas using IDW (inverse distance weighted) method. The precipitation of our study area seen in Figure .8.

### **2.7 Curvature**

Curvature reflects the morphology of the topography and can affect flooding in each area [29]. Negative, zero and positive curvatures denote concave, flat and convex surfaces [8]. The activity of runoff is associated with the concave surfaces, which are highly susceptible to flooding [30]. The curvature of our study area seen in Figure .9.

### **2.8 Watershed**

Watershed is defined as any surface area from which runoff resulting from rainfall is collected and drained through a common point. It is synonymous with a drainage basin or catchment area. A watershed may be only a few hectares as in small ponds or hundreds of square kilometres as in rivers. The watershed of our study area is seen in Figure .10.

### **2.9 Total Population and Population Density**

Total population and population density are critical parameters for assessment the risk of flash floods. The floods cause huge losses in the lives of residents and property of the local population .[3] mentioned in his paper that “the population of the governorate of Asyut reached 4,431,750 million in 2018 compared to 4,407,335 in 2017 and 4,300,748 in 2016. Population density increased from 260.8 in 2016 to 267.35 in 2017 and 268.8 person/ km<sup>2</sup> in 2018”. The population data were downloaded for free from Central Agency for Public Mobilization and Statistics, <https://www.capmas.gov.eg/> . The population data of our study area seen in Figure .11 and Figure .12.

### **2.10 Drainage Density**

Drainage density is significant in that it plays an important role in surface-runoff processes, influencing the intensity of torrential floods, the concentration, the sediment load and even the water balance in a drainage basin. Drainage density is the total length of streams in a drainage basin divided by the area of the basin. The more extensive the network of streams, the higher the drainage density will be. This measures how fast water drains into streams and rivers. . The drainage density data of our study area is seen in Figure .13.

### **2.11 Distance from Streams**

We used the DEM to extract the drainage network. Several network buffer zones were applied and drainage network classes Figure .14. When the area is close to the drainage network system, it will be more affected by floods.

### **2.12 Flow Direction and Flow Accumulation**

A flow direction raster determines the path of water will flow out of each cell of a filled elevation raster. A flow accumulation raster calculates the number of cells that flow to each cell. Flow direction raster and Flow accumulation raster are both shown in Figure .15 and Figure .16.

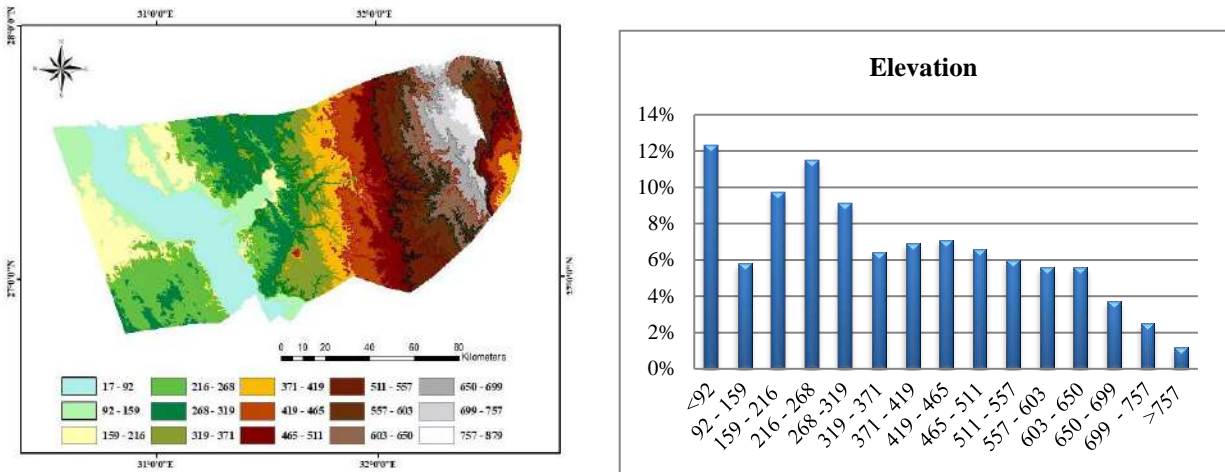


Figure 2: Elevation in Asyut

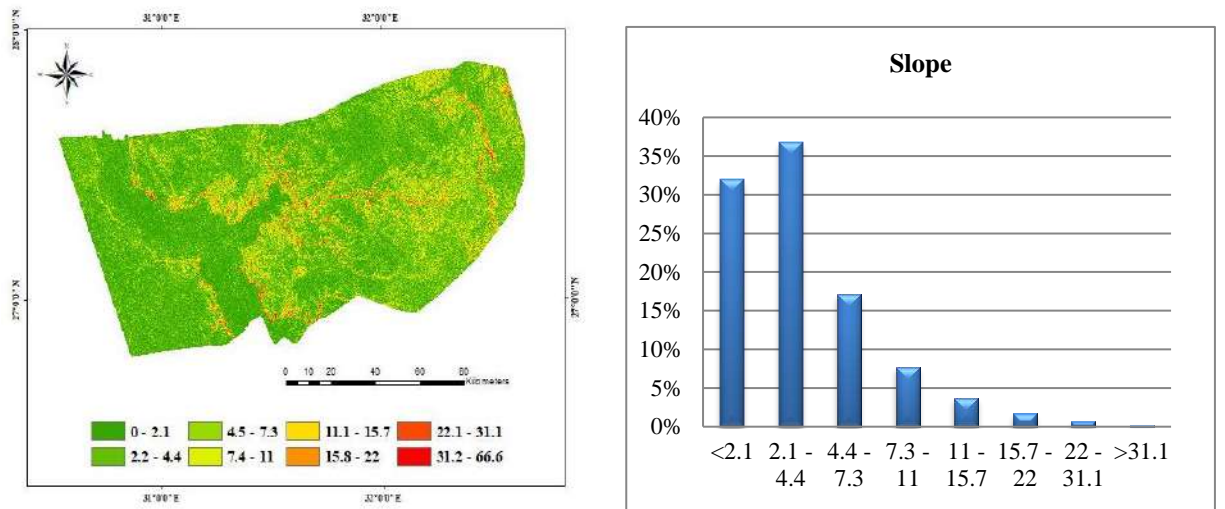


Figure 3: Slope in Asyut

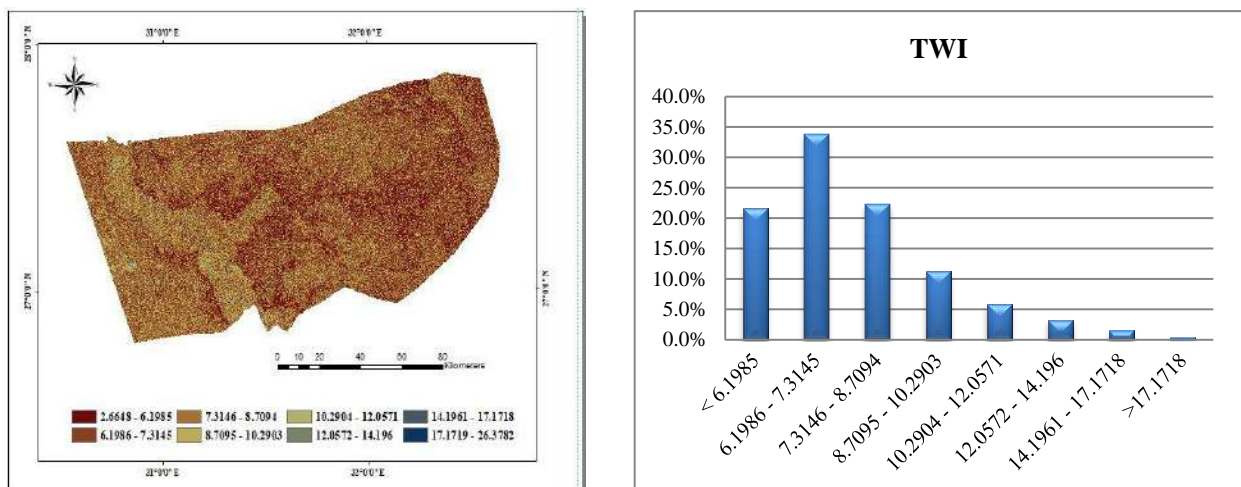


Figure 4: Topographic Wetness Index (TWI) in Asyut

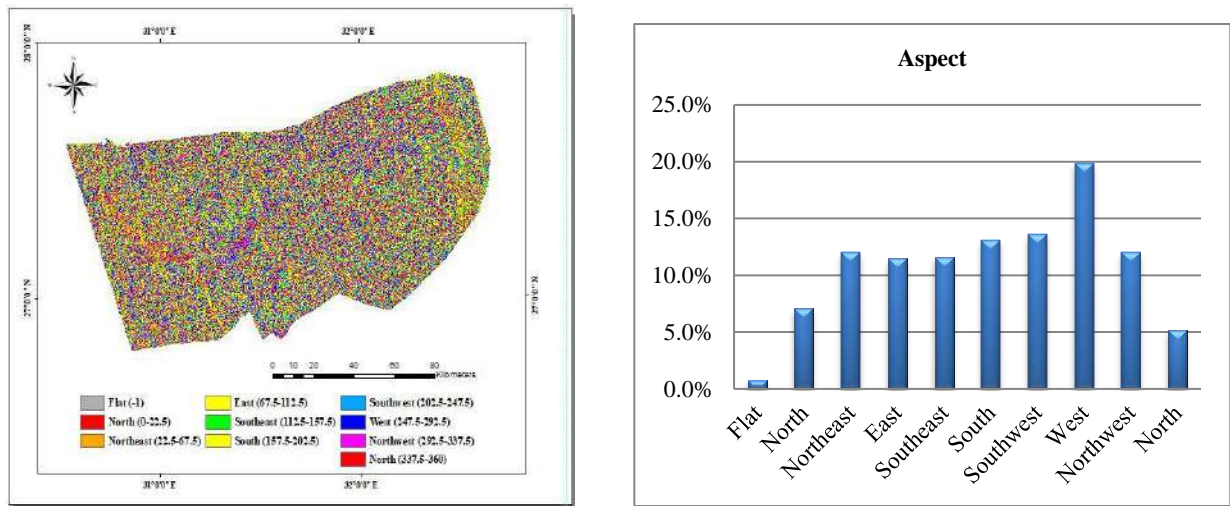


Figure 5: Aspect in Asyut

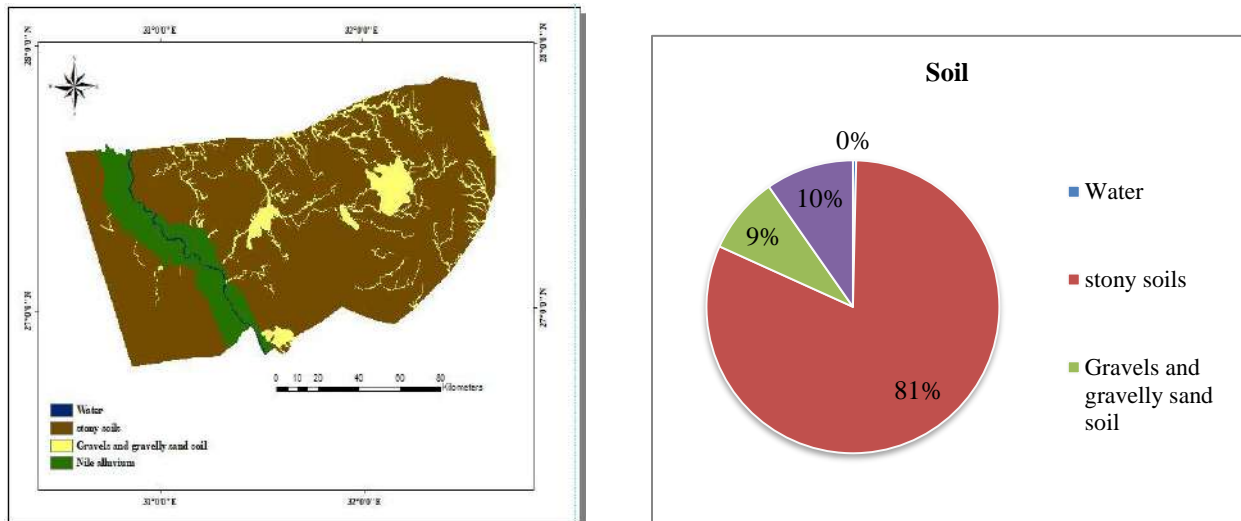


Figure 6: Soil in Asyut

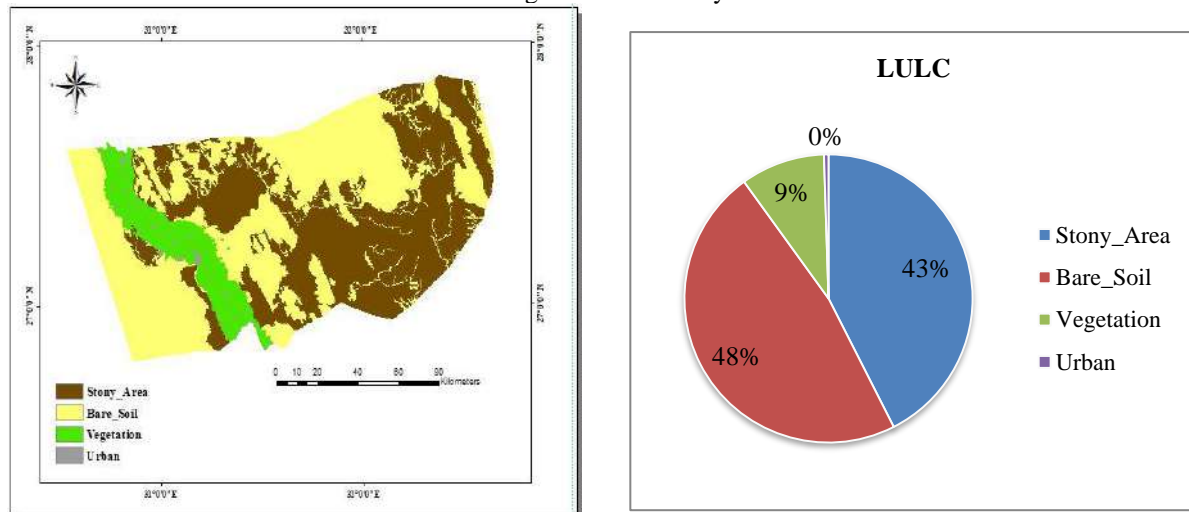


Figure 7: LULC in Asyut

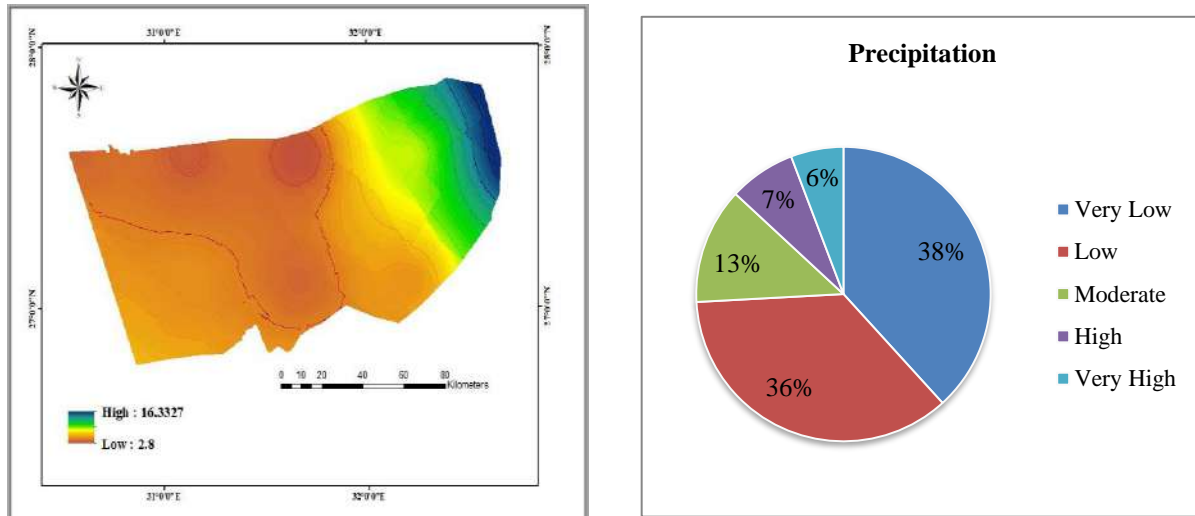


Figure 8: Precipitation in Asyut

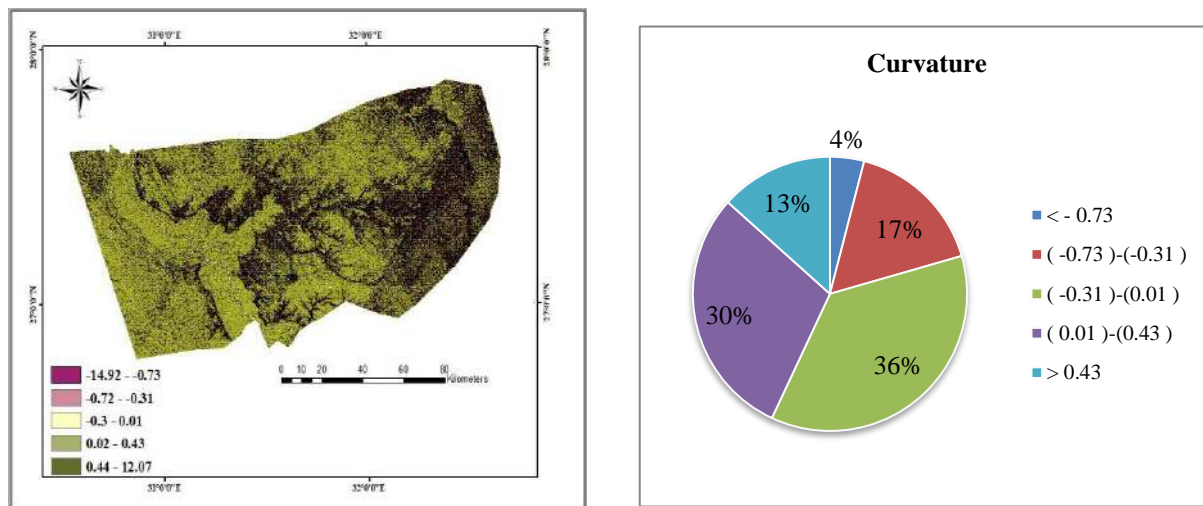


Figure 9: Curvature in Asyut

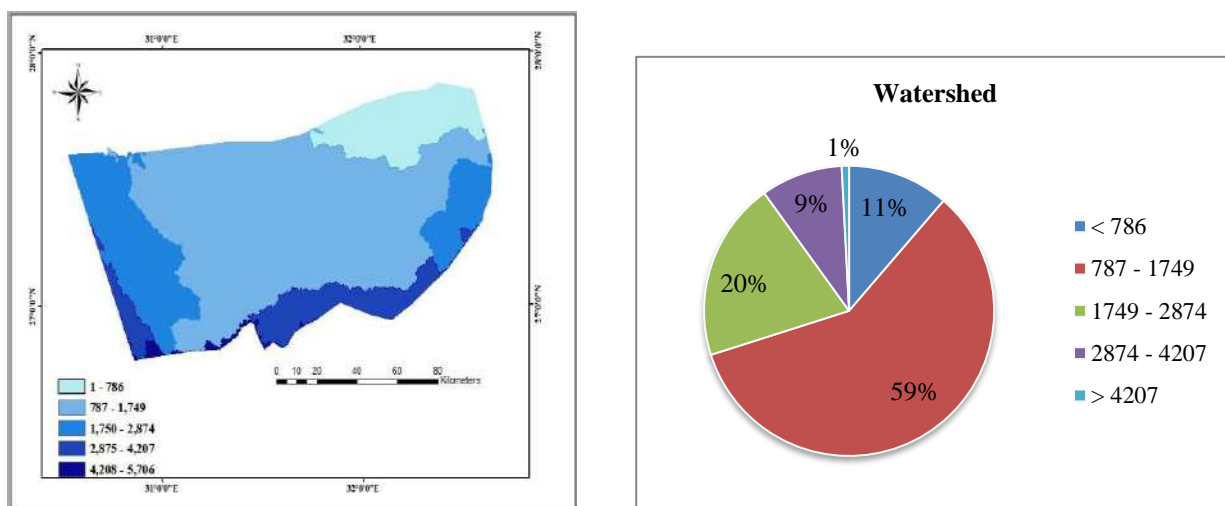


Figure 10: Watershed in Asyut

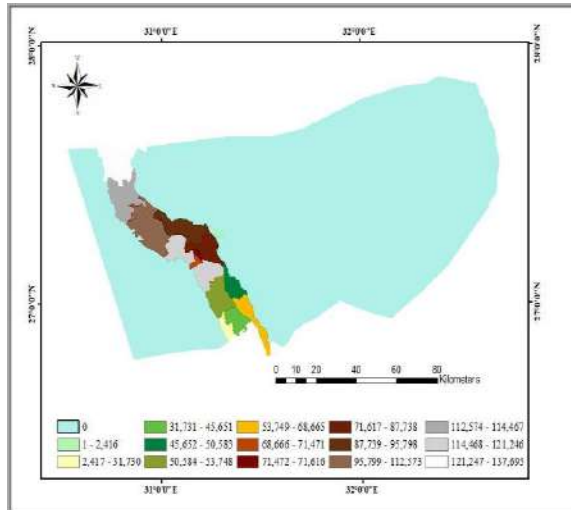


Figure 11: Total population in Asyut

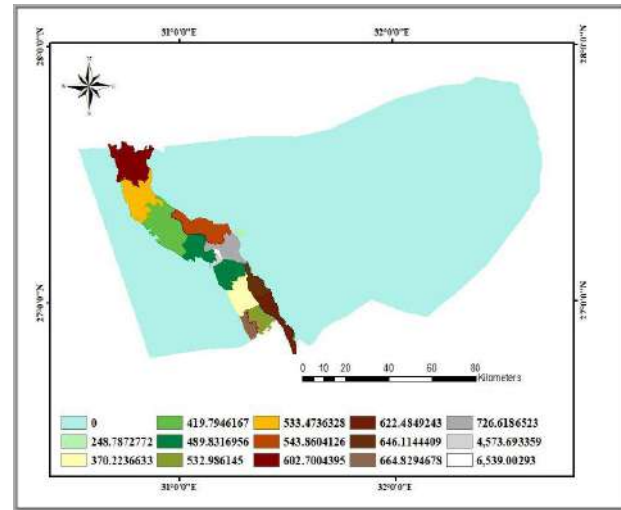


Figure 12: Population Density in Asyut

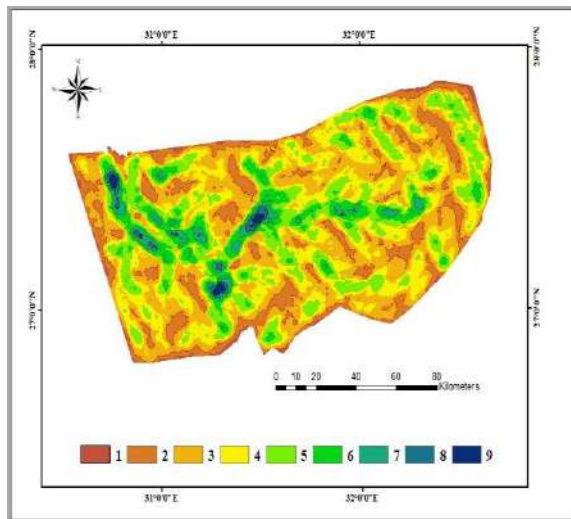


Figure 13: Drainage density in Asyut

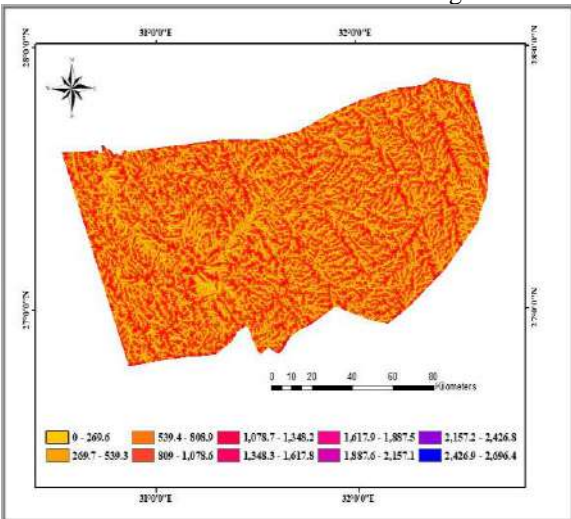
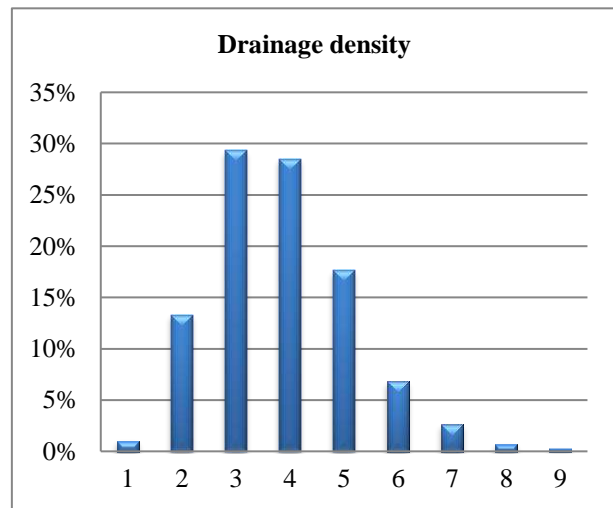
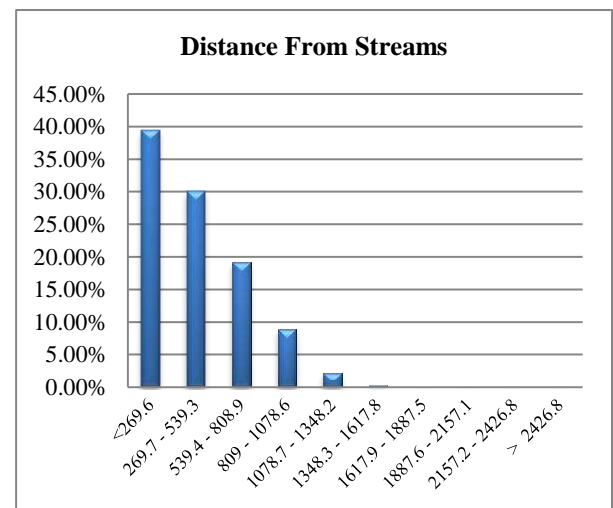


Figure 14: Distance From Streams in Asyut



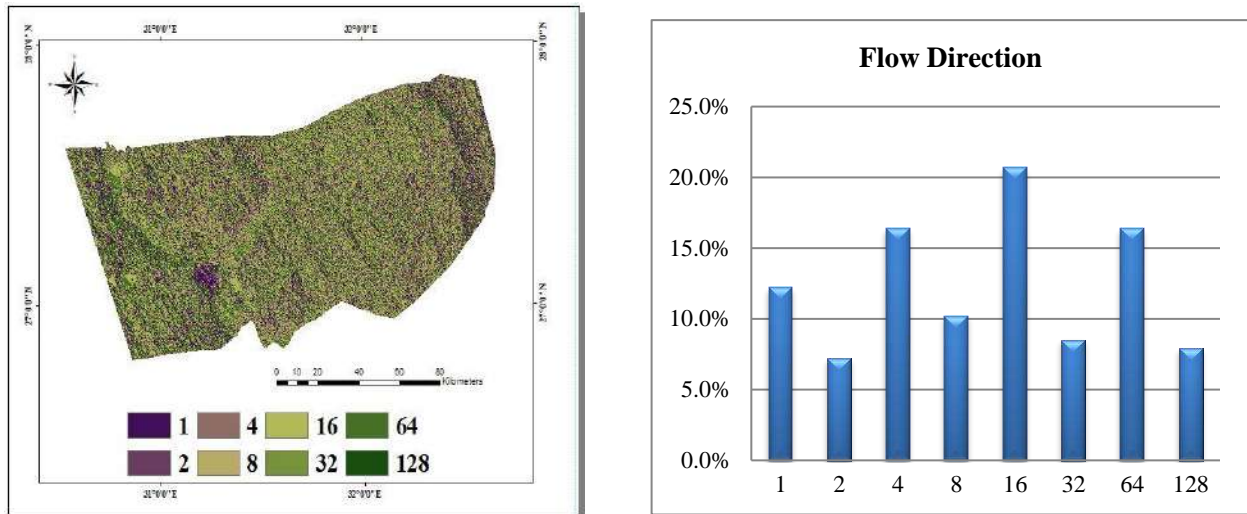


Figure 15: Flow direction in Asyut

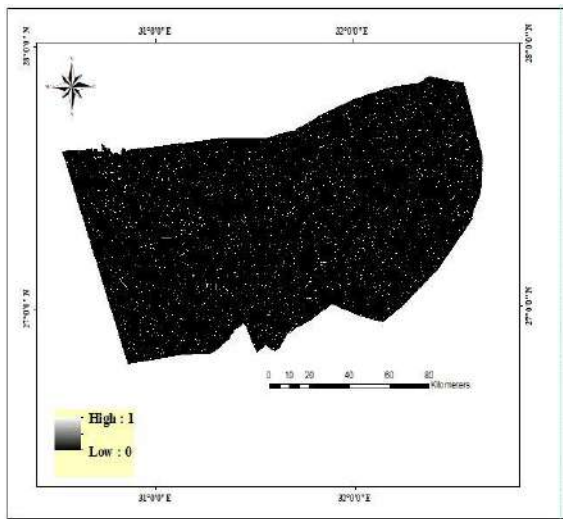


Figure 16: Flow accumulation in Asyut

### 3. Fusion of NEUTROSOPHIC PRELIMINARIES

The neutrosophic set  $N$  has three membership functions which are truth  $T_{Ne}(x)$ , indeterminacy  $I_{Ne}(x)$  and falsity  $F_{Ne}(x)$  membership functions, where  $T_{Ne}(x):X \rightarrow ]0, 1+[$ ,  $I_{Ne}(x):X \rightarrow ]0, 1+[$  and  $F_{Ne}(x):X \rightarrow ]0, 1+[$ . This set is free from restriction on the sum of  $T_{Ne}(x)$ ,  $I_{Ne}(x)$  and  $F_{Ne}(x)$ , so  $0 \leq \sup T_{Ne}(x) + \sup I_{Ne}(x) + \sup F_{Ne}(x) \leq 3^+$  [31]. In [32], An interval valued neutrosophic set INS over  $X$  has the following form  $A = \{(x, T_{Ne}(x), I_{Ne}(x), F_{Ne}(x)) : x \in X\}$  where  $T_{Ne}$  is the truth-membership function,  $I_{Ne}$  is the indeterminacy-membership function and  $F_{Ne}$  is the real falsity-membership function. For each point  $x$  in  $X$ , we have  $T_{Ne}(x) = [T_{Ne}^L(x), T_{Ne}^U(x)] \subset [0, 1]$ ,  $I_{Ne}(x) = [I_{Ne}^L(x), I_{Ne}^U(x)] \subset [0, 1]$ ,  $F_{Ne}(x) = [F_{Ne}^L(x), F_{Ne}^U(x)] \subset [0, 1]$  and  $\sup(T_{Ne}^U(x)) + \sup(I_{Ne}^U(x)) + \sup(F_{Ne}^U(x)) \leq 3$ .

Basic operations of interval valued neutrosophic numbers are as follows:

Let  $A = \langle [T_A^L, T_A^U], [I_A^L, I_A^U], [F_A^L, F_A^U] \rangle$  and  $B = \langle [T_B^L, T_B^U], [I_B^L, I_B^U], [F_B^L, F_B^U] \rangle$  be two interval valued neutrosophic numbers. Then,

$$1. A + B = \langle [T_A^L + T_B^L - T_A^L * T_B^L, T_A^U + T_B^U - T_A^U * T_B^U], [I_A^L * I_B^L, I_A^U * I_B^U], [F_A^L * F_B^L, F_A^U * F_B^U] \rangle.$$

2.  $A * B = \langle [T_A^L * T_B^L, T_A^U * T_B^U], [I_A^L + I_B^L - I_A^L * I_B^L, I_A^U + I_B^U - I_A^U * I_B^U], [F_A^L + F_B^L - F_A^L * F_B^L, F_A^U + F_B^U - F_A^U * F_B^U] \rangle$ .
3.  $n * A = \langle [1 - (1 - T_A^L)^n, 1 - (1 - T_A^U)^n], [(I_A^L)^n, (I_A^U)^n], [(F_A^L)^n, (F_A^U)^n] \rangle$ .
4.  $A^n = \langle [(T_A^L)^n, (T_A^U)^n], [1 - (1 - I_A^L)^n, 1 - (1 - I_A^U)^n], [1 - (1 - F_A^L)^n, 1 - (1 - F_A^U)^n] \rangle$ .

#### 4. PROPOSED FUSION NEUTROSOPHIC EXTENDED DECISION-MAKING TRIAL AND EVALUATION LABORATORY (N-DEMATEL) TECHNIQUE

There are various methods for evaluating the weights of decision attributes as AHP [33], FARE [34], entropy [35]. DEMATEL was first developed by the Science and Human affairs Program of the Battelle Memorial Institute of Geneva[20]. DEMATEL is an effective way to identify the components of the cause chain in a complex system [21]. The DEMATEL technique has the following advantages: (1) It effectively analyzes the mutual influences (direct and indirect effects) between different factors and understands the complex cause-and-effect relationships in a decision-making problem.(2)It is able to visualize the relationships among the factors via IRM and enable the decision maker to have a clear understanding of the factors that influence each other.(3) DEMATEL can be used not only to determine the order of alternatives, but also to detect important evaluation criteria and measure the weights of the evaluation criteria. [21] mentioned that the possible disadvantages of the DEMATEL technique may be the following: (1) It determines the order of alternatives on the basis of the interrelationships among them; But other criteria were not incorporated into the decision-making problem.(2) The relative weights of experts are not taken into account when aggregating experts' subjective judgments in group assessments.(3) It cannot take into account the level of ambition of the alternatives as in the GRA and VIKOR methods or obtain a partial ranking of the alternatives as in the ELECTRE approach.

The procedure for determination of weights by N- DEMATEL is stated in the steps below:

**Step 1:** Let decision makers begin to evaluate criteria according to their expected significances using the neutrosophic scale as appears in Table 2

Table 2: The linguistic values and its corresponding neutrosophic values for evaluation process

Linguistic Variable	Corresponding Neutrosophic Values (NV <sub>s</sub> )
Absolutely low Significance	$\langle [0.5,0.6], [0.35,0.45], [0.4,0.5] \rangle$
Extremely low Significance	$\langle [0.55,0.65], [0.3,0.4], [0.35,0.45] \rangle$
Very Low Significance	$\langle [0.6,0.7], [0.25,0.35], [0.3,0.4] \rangle$
Medium Low Significance	$\langle [0.65,0.75], [0.2,0.3], [0.25,0.35] \rangle$
Low Significance	$\langle [0.7,0.8], [0.15,0.25], [0.2,0.3] \rangle$
Equally significance	$\langle [0.5,0.5], [0.5,0.5], [0.5,0.5] \rangle$
High Significance	$\langle [0.75,0.85], [0.1,0.2], [0.15,0.25] \rangle$
Medium High Significance	$\langle [0.8,0.9], [0.05,0.1], [0.1,0.2] \rangle$
Very High Significance	$\langle [0.9,0.95], [0,0.05], [0.05,0.15] \rangle$
Extremely High Significance	$\langle [0.95,1], [0,0], [0,0.1] \rangle$
Absolutely High Significance	$\langle [1,1], [0,0], [0,0] \rangle$

The previous linguistic variables are used by decision makers to clear their preferences.

**Step 2 :** Generating the direct relation matrix:

This matrix is obtained from previous step (1), i.e., the integrating of all averaged opinions of experts. An initial direct relation matrix A is a  $n \times n$  matrix obtained by pairwise comparisons.

**Step 3 :** Normalizing the direct relation matrix.

The normalized direct relation matrix can be obtained using the equation:

$$D = A \times M, \text{ where } M = \frac{1}{\text{MAX}_{1 \leq i \leq n} \sum_{j=1}^n a_{ij}} \quad (1)$$

**Step 4:** Attaining the total relation matrix.

This step requires use of the Microsoft Excel software. The total relation matrix is acquired using the formula (2) from the generalized direct relation matrix D. A total relation matrix (T),

in which (I) denotes the identity matrix, is shown as follows:

$$T = D \times (I - D)^{-1} \quad (2)$$

**Step 5:** Obtaining the sum of rows and columns.

The sum of rows is denoted by (D), and the sum of columns is denoted by (R). Calculate R+D and R-D from the total-influence matrix using the formula (3) and (4) .

$$D = \sum_{j=1}^n a_{ij}, i = 1,2,3, \dots, n \quad (3)$$

$$R = \sum_{i=1}^n a_{ij}, j = 1,2,3, \dots, n \quad (4)$$

**Step 6 :** Drawing cause and effect diagram

The causal diagram is obtained by the horizontal axes is presented by (D+R) and the vertical axes (D-R) which is a degree of relation and it depicts the steps of proposed model in Figure 17.

**Step 7 :** calculate the weights of criteria .

The priority weight of each criterion can be calculated as follows:

$$W_i = \frac{D_i + R_i}{\sum_{i=1}^n (D_i + R_i)}, i = 1,2,3, \dots, n \quad (5)$$

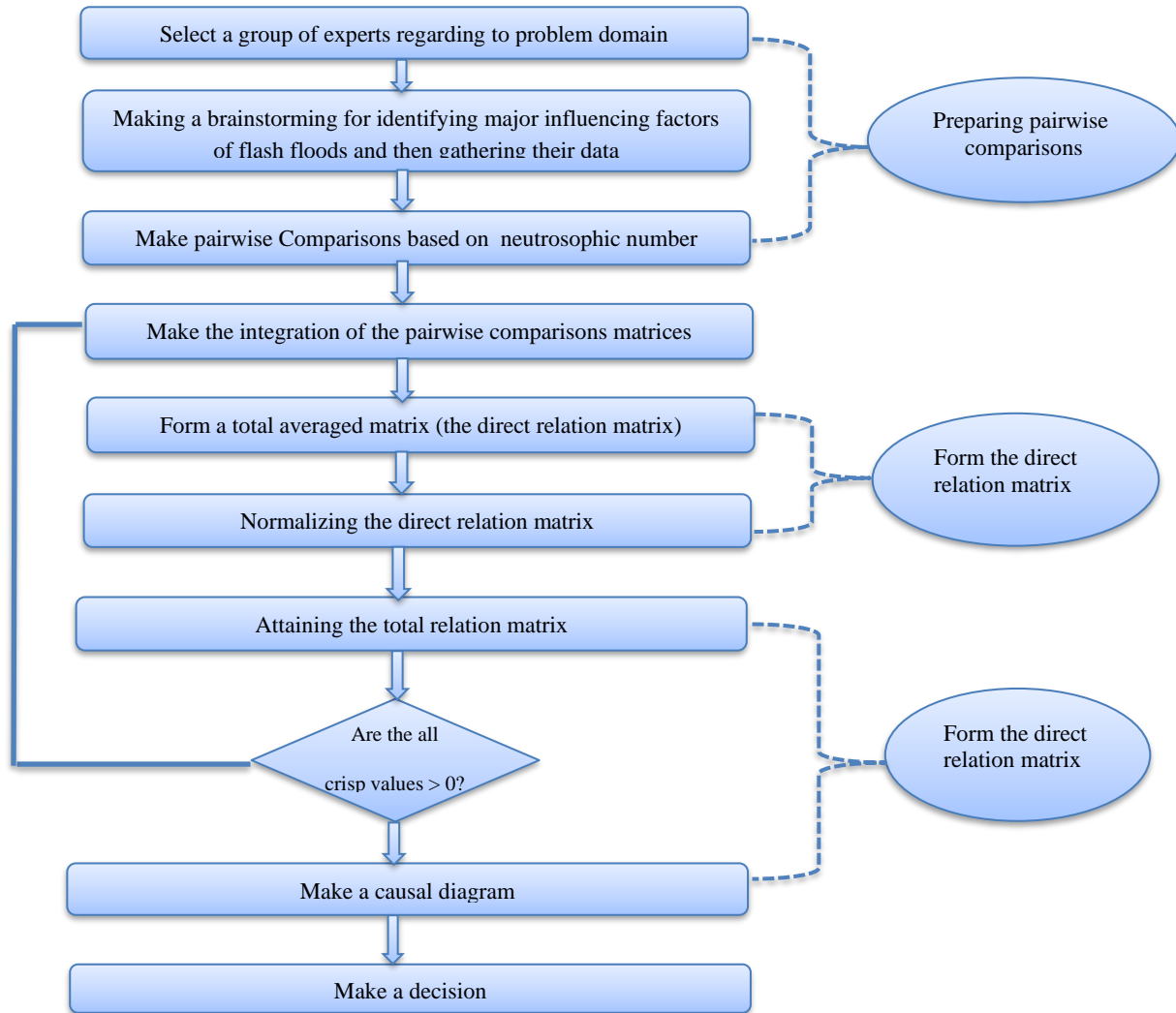


Figure 17: Schematic diagram of DEMATEL in neutrosophic environment

### 5. Fusion of NEUTROSOPHIC N-DEMATEL ANALYSIS FOR WEIGHTING FLOOD INFLUENCING FACTORS

In our study, we are the first to propose an extended single interval valued neutrosophic DEMATEL technique based on GIS for analyzing flash floods. The N-DEMATEL used to obtain weights of flood influencing factors and combined into the GIS - environment to create flood susceptibility maps. The integration of GIS-environment with neutrosophic DEMATEL analysis provides more flexibility for to assess the causative agents of flooding. The general framework of proposed model for analyzing flash floods appears in Figure .18.

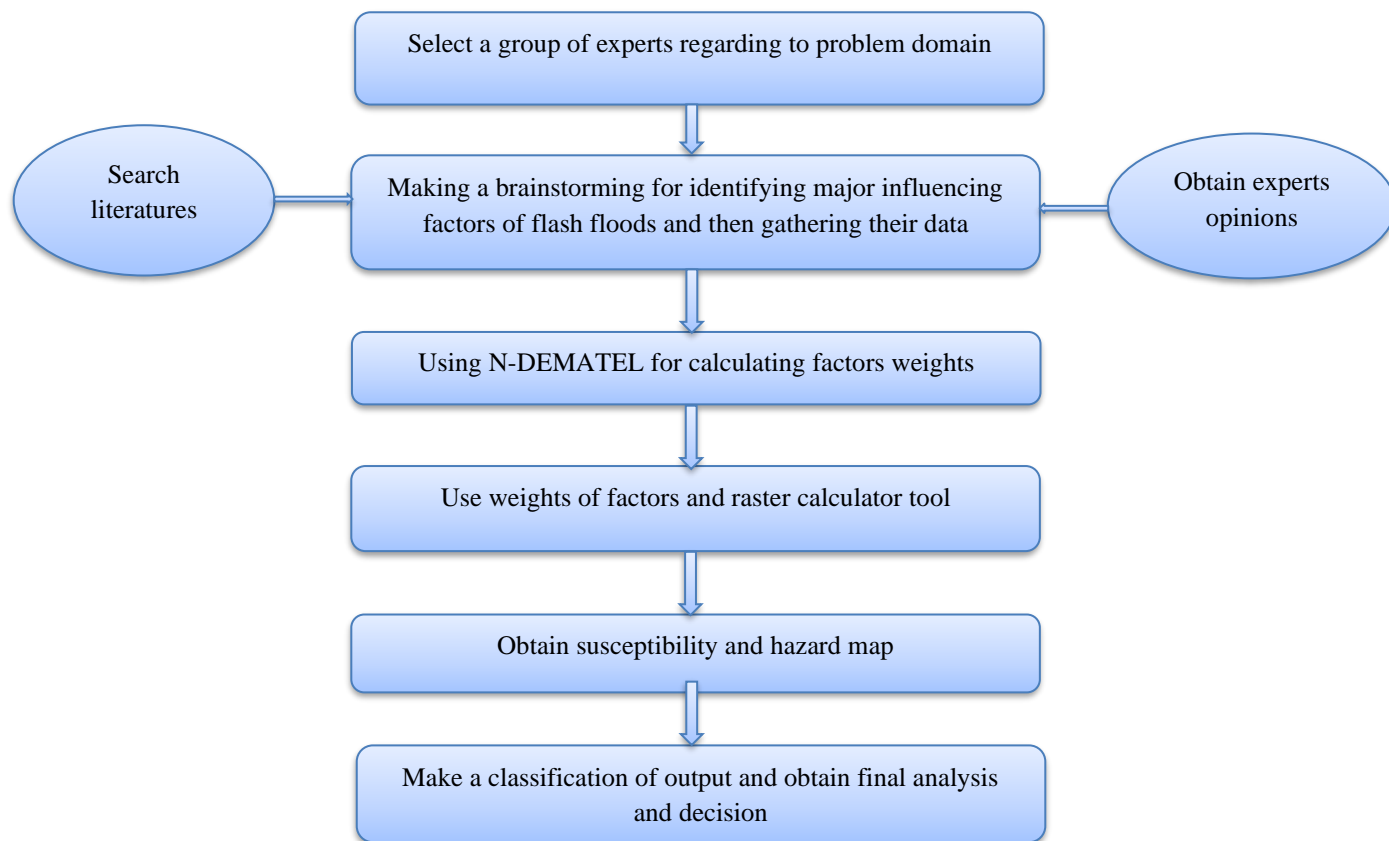


Figure 18: Study methodology

Since in our study area we discuss various factors related to flash flooding as elevation, slope, topographic wetness index, distance from the stream, flow accumulation, aspect, flow direction, soil, land cover, watershed, curvature, drainage density, total population, population density and precipitation. So, let us now use proposed algorithm for calculating its weights and then make analysis of flash floods as follows:

**Step 1:** Previous studies were used to evaluate criteria using neutrosophic linguistic variables which presented in Table 2 [3, 7-9] and obtained data which presented in Table 3.

Table 3 :The neutrosophic values for evaluating criteria : C1(Population Density), C2(Total Population), C3(Precipitation), C4(Distance From Stream), C5(DEM), C6(DrainageDensity), C7(Soil), C8(LULC), C9(Slope), C10(Flow Direction), C11(Flow Accumulation), C12(TWI), C13(Curvature), C14(Aspect), C15(Watershed).

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15
C1	ES	HS	HS	MH S	MH S	MH S	EH S	VH S	MH S	EH S	EH S	EH S	EH S	AH S	AH S
C2	LS	ES	HS	MH S	MH S	MH S	EH S	VH S	MH S	EH S	EH S	EH S	EH S	AH S	AH S
C3	LS	LS	ES	VH S	MH S	HS	MH S	MH S	HS	EH S	VH S	EH S	EH S	AH S	AH S
C4	ML S	ML S	VL S	ES	HS	MH S	HS	VH S	MH S	EH S	EH S	EH S	EH S	AH S	AH S
C5	ML S	ML S	ML S	LS	ES	MH S	HS	MH S	MH S	VH S	VH S	EH S	VH S	VH S	AH S
C6	ML S	ML S	LS	ML S	ML S	ES	MH S	VH S	MH S	EH S	EH S	EH S	EH S	AH S	AH S

C7	ELS	ELS	ML S	LS	LS	ML S	ES	HS	HS	MH S	HS	VH S	EH S	VH S	VH S
C8	VL S	VL S	ML S	VL S	ML S	VL S	LS	ES	HS	MH S	MH S	VH S	EH S	VH S	VH S
C9	ML S	ML S	LS	ML S	ML S	ML S	LS	LS	ES	HS	HS	MH S	MH S	VH S	VH S
C1 0	ELS	ELS	ELS	ELS	VL S	ELS	ML S	ML S	LS	ES	HS	MH S	MH S	VH S	VH S
C1 1	ELS	ELS	VL S	ELS	VL S	ELS	LS	ML S	LS	LS	ES	MH S	MH S	VH S	VH S
C1 2	ELS	ELS	ELS	ELS	ELS	ELS	VL S	VL S	ML S	ML S	ML S	ES	HS	MH S	MH S
C1 3	ELS	ELS	ELS	ELS	VL S	ELS	ELS	ELS	ML S	ML S	ML S	LS	ES	MH S	MH S
C1 4	AL S	AL S	AL S	AL S	VL S	AL S	VL S	VL S	VL S	VL S	VL S	ML S	ML S	ES	VH S
C1 5	AL S	AL S	AL S	AL S	AL S	AL S	VL S	VL S	VL S	VL S	VL S	ML S	ML S	VL S	ES

Then, the single-valued interval neutrosophic fuzzy direct-relation decision matrix is formed as  $A = \{ \langle x, T_{Ne}(x), I_{Ne}(x), F_{Ne}(x) : x \in X \rangle \}$  where  $T_{Ne}$  is the truth-membership function,  $I_{Ne}$  is the indeterminacy-membership function and  $F_{Ne}$  is the real falsity-membership function as presented in Table 4.

**Step2 :** Normalize the direct-relation decision matrix A to  $D = \langle [T_D^L, T_D^U], [I_D^L, I_D^U], [F_D^L, F_D^U] \rangle$ ,  $T_D^L = \frac{T_A^L}{K}$ ,  $T_D^U = \frac{T_A^U}{K}$ ,  $K = \max \left\{ \max_{1 \leq i \leq n} \sum_{j=1}^n T_{A_{ij}}^L, \max_{1 \leq j \leq n} \sum_{i=1}^n T_{A_{ij}}^U \right\}$ .  $I_D^L = \frac{I_A^L}{K}$ ,  $I_D^U = \frac{I_A^U}{K}$ ,  $K = \max \left\{ \max_{1 \leq i \leq n} \sum_{j=1}^n I_{A_{ij}}^L, \max_{1 \leq j \leq n} \sum_{i=1}^n I_{A_{ij}}^U \right\}$ .  $F_D^L = \frac{F_A^L}{K}$ ,  $F_D^U = \frac{F_A^U}{K}$ ,  $K = \max \left\{ \max_{1 \leq i \leq n} \sum_{j=1}^n F_{A_{ij}}^L, \max_{1 \leq j \leq n} \sum_{i=1}^n F_{A_{ij}}^U \right\}$  see (Appendix A).

**Step3 :** Calculate the total-relation matrix  $\tilde{D}$ , which can be calculated by using the six crisp

Normalize direct-relation decision matrix D where  $\tilde{D} = \langle [T_{\tilde{D}}^L, T_{\tilde{D}}^U], [I_{\tilde{D}}^L, I_{\tilde{D}}^U], [F_{\tilde{D}}^L, F_{\tilde{D}}^U] \rangle$ ,  
 $T_{\tilde{D}}^L = T_D^L \times (I - T_D^L)^{-1}$ ,  $T_{\tilde{D}}^U = T_D^U \times (I - T_D^U)^{-1}$ ,  $I_{\tilde{D}}^L = I_D^L \times (I - I_D^L)^{-1}$ ,  $I_{\tilde{D}}^U = I_D^U \times (I - I_D^U)^{-1}$ ,  $F_{\tilde{D}}^L = F_D^L \times (I - F_D^L)^{-1}$ ,  $F_{\tilde{D}}^U = F_D^U \times (I - F_D^U)^{-1}$  as presented in Table 5.

Table 4: single-valued interval neutrosophic fuzzy direct-relation decision matrix

	C1	C2	C3
C1	$\langle [0.5,0.5],[0.5,0.5],[0.5,0.5] \rangle$	$\langle [0.75,0.85],[0.1,0.2],[0.15,0.25] \rangle$	$\langle [0.75,0.85],[0.1,0.2],[0.15,0.25] \rangle$
C2	$\langle [0.7,0.8],[0.15,0.25],[0.2,0.3] \rangle$	$\langle [0.5,0.5],[0.5,0.5],[0.5,0.5] \rangle$	$\langle [0.75,0.85],[0.1,0.2],[0.15,0.25] \rangle$
C3	$\langle [0.7,0.8],[0.15,0.25],[0.2,0.3] \rangle$	$\langle [0.7,0.8],[0.15,0.25],[0.2,0.3] \rangle$	$\langle [0.5,0.5],[0.5,0.5],[0.5,0.5] \rangle$
C4	$\langle [0.65,0.75],[0.2,0.3],[0.25,0.35] \rangle$	$\langle [0.65,0.75],[0.2,0.3],[0.25,0.35] \rangle$	$\langle [0.6,0.7],[0.25,0.35],[0.3,0.4] \rangle$
C5	$\langle [0.65,0.75],[0.2,0.3],[0.25,0.35] \rangle$	$\langle [0.65,0.75],[0.2,0.3],[0.25,0.35] \rangle$	$\langle [0.65,0.75],[0.2,0.3],[0.25,0.35] \rangle$
C6	$\langle [0.65,0.75],[0.2,0.3],[0.25,0.35] \rangle$	$\langle [0.65,0.75],[0.2,0.3],[0.25,0.35] \rangle$	$\langle [0.7,0.8],[0.15,0.25],[0.2,0.3] \rangle$

<b>C7</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.65,0.75],[0.2,0.3],[0.25,0.35]> >
<b>C8</b>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]> >
<b>C9</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]> >	<[0.65,0.75],[0.2,0.3],[0.25,0.35]> >	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>
<b>C10</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >
<b>C11</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>
<b>C12</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >
<b>C13</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >
<b>C14</b>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>
<b>C15</b>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>

Table 4 :(continued)

	<b>C4</b>	<b>C5</b>	<b>C6</b>
<b>C1</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C2</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C3</b>	<[0.9,0.95],[0,0.05],[0.05,0.15]> >	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>
<b>C4</b>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.75,0.85],[0.1,0.2],[0.1,0.25]> >	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C5</b>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]> >	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C6</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]> >	<[0.65,0.75],[0.2,0.3],[0.25,0.35]> >	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>
<b>C7</b>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]> >	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>
<b>C8</b>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]> >	<[0.65,0.75],[0.2,0.3],[0.2,0.35]> >	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>
<b>C9</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]> >	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>
<b>C10</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]>
<b>C11</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]>
<b>C12</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.55,0.65],[0.3,0.4],[0.35,0.45]>
<b>C13</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]> >	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]>
<b>C14</b>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]> >	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>
<b>C15</b>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]> >	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>	<[0.5,0.6],[0.35,0.45],[0.4,0.5]>

Table 4 :(continued)

	<b>C7</b>	<b>C8</b>	<b>C9</b>

<b>C1</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C2</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C3</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>
<b>C4</b>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C5</b>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C6</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C7</b>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>
<b>C8</b>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>
<b>C9</b>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>
<b>C10</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>
<b>C11</b>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>
<b>C12</b>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>
<b>C13</b>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]>	<[0.55,0.65],[0.3,0.4],[0.35,0.45]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>
<b>C14</b>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>
<b>C15</b>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>

Table 4 :(continued)

	<b>C10</b>	<b>C11</b>	<b>C12</b>
<b>C1</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>
<b>C2</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>
<b>C3</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.95,1],[0,0],[0,0.1]>
<b>C4</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>
<b>C5</b>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.95,1],[0,0],[0,0.1]>
<b>C6</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>	<[0.95,1],[0,0],[0,0.1]>
<b>C7</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C8</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C9</b>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C10</b>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C11</b>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C12</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>
<b>C13</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.7,0.8],[0.15,0.25],[0.2,0.3]>

<b>C1</b>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>
<b>4</b>	>		
<b>C1</b>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>
<b>5</b>	>		

Table 4 :(continued)

	<b>C13</b>	<b>C14</b>	<b>C15</b>
<b>C1</b>	<[0.95,1],[0,0],[0,0.1]>	<[1,1],[0,0],[0,0]>	<[1,1],[0,0],[0,0]>
<b>C2</b>	<[0.95,1],[0,0],[0,0.1]>	<[1,1],[0,0],[0,0]>	<[1,1],[0,0],[0,0]>
<b>C3</b>	<[0.95,1],[0,0],[0,0.1]>	<[1,1],[0,0],[0,0]>	<[1,1],[0,0],[0,0]>
<b>C4</b>	<[0.95,1],[0,0],[0,0.1]>	<[1,1],[0,0],[0,0]>	<[1,1],[0,0],[0,0]>
<b>C5</b>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[1,1],[0,0],[0,0]>
<b>C6</b>	<[0.95,1],[0,0],[0,0.1]>	<[1,1],[0,0],[0,0]>	<[1,1],[0,0],[0,0]>
<b>C7</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C8</b>	<[0.95,1],[0,0],[0,0.1]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C9</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C10</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C11</b>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C12</b>	<[0.75,0.85],[0.1,0.2],[0.15,0.25]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C13</b>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>	<[0.8,0.9],[0.05,0.1],[0.1,0.2]>
<b>C14</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>	<[0.9,0.95],[0,0.05],[0.05,0.15]>
<b>C15</b>	<[0.65,0.75],[0.2,0.3],[0.25,0.35]>	<[0.6,0.7],[0.25,0.35],[0.3,0.4]>	<[0.5,0.5],[0.5,0.5],[0.5,0.5]>

Table 5 : The total-relation matrix T

	<b>C1</b>	<b>C2</b>	<b>C3</b>
<b>C1</b>	<[0.20,0.35],[0.10,0.11],[0.08,0.11]>	<[0.21,0.38],[0.02,0.05],[0.03,0.07]>	<[0.22,0.39],[0.02,0.05],[0.03,0.07]>
<b>C2</b>	<[0.21,0.37],[0.03,0.06],[0.04,0.08]>	<[0.20,0.35],[0.10,0.11],[0.08,0.11]>	<[0.22,0.39],[0.02,0.05],[0.03,0.07]>
<b>C3</b>	<[0.20,0.36],[0.03,0.07],[0.04,0.09]>	<[0.21,0.37],[0.03,0.07],[0.04,0.09]>	<[0.20,0.35],[0.10,0.11],[0.08,0.12]>
<b>C4</b>	<[0.20,0.35],[0.05,0.08],[0.05,0.10]>	<[0.20,0.36],[0.05,0.08],[0.05,0.10]>	<[0.20,0.36],[0.05,0.09],[0.06,0.10]>
<b>C5</b>	<[0.19,0.35],[0.05,0.09],[0.05,0.11]>	<[0.19,0.35],[0.05,0.09],[0.05,0.11]>	<[0.20,0.36],[0.05,0.09],[0.05,0.10]>
<b>C6</b>	<[0.20,0.35],[0.05,0.08],[0.05,0.10]>	<[0.20,0.35],[0.05,0.08],[0.05,0.10]>	<[0.21,0.37],[0.04,0.07],[0.04,0.09]>
<b>C7</b>	<[0.18,0.33],[0.07,0.12],[0.08,0.14]>	<[0.18,0.33],[0.07,0.12],[0.08,0.14]>	<[0.19,0.34],[0.05,0.10],[0.06,0.12]>
<b>C8</b>	<[0.18,0.33],[0.06,0.12],[0.07,0.13]>	<[0.18,0.33],[0.06,0.11],[0.07,0.13]>	<[0.19,0.34],[0.05,0.10],[0.06,0.12]>
<b>C9</b>	<[0.18,0.33],[0.06,0.11],[0.06,0.13]>	<[0.18,0.33],[0.06,0.11],[0.06,0.13]>	<[0.19,0.34],[0.04,0.10],[0.05,0.12]>

<b>C10</b>	<[0.16,0.30],[0.08,0.14],[0.08,0.16]>	<[0.16,0.31],[0.08,0.14],[0.08,0.15]>	<[0.17,0.31],[0.08,0.14],[0.08,0.15]>
<b>C11</b>	<[0.16,0.31],[0.08,0.14],[0.08,0.15]>	<[0.16,0.31],[0.08,0.14],[0.08,0.15]>	<[0.17,0.32],[0.07,0.13],[0.07,0.14]>
<b>C12</b>	<[0.16,0.29],[0.09,0.16],[0.09,0.17]>	<[0.16,0.29],[0.09,0.16],[0.09,0.17]>	<[0.16,0.30],[0.09,0.15],[0.09,0.16]>
<b>C13</b>	<[0.15,0.29],[0.09,0.16],[0.09,0.17]>	<[0.15,0.29],[0.09,0.16],[0.09,0.17]>	<[0.16,0.30],[0.09,0.16],[0.09,0.16]>
<b>C14</b>	<[0.15,0.28],[0.11,0.18],[0.11,0.19]>	<[0.15,0.28],[0.11,0.18],[0.10,0.19]>	<[0.15,0.28],[0.10,0.18],[0.10,0.18]>
<b>C15</b>	<[0.14,0.27],[0.11,0.20],[0.11,0.20]>	<[0.14,0.27],[0.11,0.19],[0.11,0.19]>	<[0.14,0.28],[0.11,0.19],[0.11,0.19]>

Table 5 :(continued)

	<b>C4</b>	<b>C5</b>	<b>C6</b>
<b>C1</b>	<[0.23,0.40],[0.01,0.03],[0.02,0.06]>	<[0.23,0.41],[0.01,0.03],[0.02,0.06]>	<[0.23,0.40],[0.01,0.03],[0.02,0.06]>
<b>C2</b>	<[0.23,0.390.01,0.03],[0.02,0.06]>	<[0.23,0.40],[0.01,0.03],[0.02,0.06]>	<[0.23,0.40],[0.01,0.03],[0.02,0.06]>
<b>C3</b>	<[0.23,0.39],[0.00,0.03],[0.01,0.06]>	<[0.23,0.40],[0.01,0.03],[0.02,0.07]>	<[0.22,0.39],[0.02,0.05],[0.03,0.07]>
<b>C4</b>	<[0.20,0.35],[0.10,0.11],[0.08,0.11]>	<[0.22,0.39],[0.02,0.05],[0.03,0.08]>	<[0.22,0.38],[0.01,0.03],[0.02,0.07]>
<b>C5</b>	<[0.21,0.37],[0.03,0.07],[0.04,0.09]>	<[0.20,0.36],[0.10,0.11],[0.09,0.12]>	<[0.21,0.38],[0.01,0.04],[0.03,0.08]>
<b>C6</b>	<[0.21,0.37],[0.04,0.07],[0.05,0.09]>	<[0.21,0.38],[0.04,0.07],[0.05,0.09]>	<[0.20,0.35],[0.10,0.11],[0.08,0.11]>
<b>C7</b>	<[0.19,0.35],[0.04,0.08],[0.05,0.11]>	<[0.20,0.36],[0.04,0.08],[0.05,0.10]>	<[0.19,0.35],[0.05,0.09],[0.05,0.11]>
<b>C8</b>	<[0.19,0.34],[0.06,0.10],[0.06,0.12]>	<[0.19,0.35],[0.05,0.09],[0.05,0.11]>	<[0.19,0.34],[0.06,0.10],[0.06,0.12]>
<b>C9</b>	<[0.19,0.34],[0.05,0.10],[0.06,0.12]>	<[0.19,0.35],[0.05,0.10],[0.06,0.12]>	<[0.19,0.35],[0.05,0.10],[0.06,0.12]>
<b>C10</b>	<[0.17,0.32],[0.07,0.13],[0.08,0.14]>	<[0.18,0.33],[0.06,0.11],[0.07,0.13]>	<[0.17,0.32],[0.07,0.12],[0.08,0.14]>
<b>C11</b>	<[0.17,0.32],[0.07,0.13],[0.08,0.14]>	<[0.18,0.33],[0.06,0.11],[0.07,0.13]>	<[0.17,0.32],[0.07,0.12],[0.08,0.14]>
<b>C12</b>	<[0.16,0.30],[0.08,0.14],[0.08,0.16]>	<[0.17,0.31],[0.08,0.14],[0.08,0.15]>	<[0.16,0.31],[0.08,0.14],[0.08,0.15]>
<b>C13</b>	<[0.16,0.30],[0.08,0.14],[0.09,0.16]>	<[0.17,0.31],[0.07,0.13],[0.08,0.15]>	<[0.16,0.30],[0.08,0.14],[0.08,0.16]>
<b>C14</b>	<[0.15,0.29],[0.10,0.16],[0.10,0.17]>	<[0.16,0.30],[0.08,0.14],[0.08,0.15]>	<[0.15,0.29],[0.10,0.16],[0.10,0.17]>
<b>C15</b>	<[0.15,0.28],[0.10,0.17],[0.10,0.18]>	<[0.15,0.29],[0.10,0.17],[0.10,0.18]>	<[0.15,0.28],[0.10,0.17],[0.10,0.18]>

Table 5 :(continued)

	<b>C7</b>	<b>C8</b>	<b>C9</b>
<b>C1</b>	<[0.26,0.44],[0.00,0.01],[0.00,0.04]>	<[0.26,0.43],[0.00,0.01],[0.01,0.05]>	<[0.25,0.43],[0.01,0.03],[0.02,0.06]>

<b>C2</b>	<[0.26,0.43],[0.00,0.01],[0.00,0.04]>	<[0.26,0.43],[0.00,0.01],[0.01,0.05]>	<[0.25,0.43],[0.01,0.03],[0.02,0.06]>
<b>C3</b>	<[0.24,0.42],[0.01,0.03],[0.02,0.06]>	<[0.24,0.42],[0.01,0.03],[0.02,0.06]>	<[0.24,0.42],[0.02,0.05],[0.03,0.07]>
<b>C4</b>	<[0.23,0.41],[0.02,0.05],[0.03,0.07]>	<[0.25,0.42],[0.00,0.02],[0.01,0.05]>	<[0.24,0.42],[0.01,0.03],[0.02,0.06]>
<b>C5</b>	<[0.23,0.40],[0.02,0.05],[0.03,0.08]>	<[0.23,0.41],[0.01,0.03],[0.02,0.07]>	<[0.23,0.41],[0.01,0.04],[0.02,0.07]>
<b>C6</b>	<[0.23,0.41],[0.01,0.03],[0.02,0.06]>	<[0.24,0.41],[0.00,0.02],[0.01,0.05]>	<[0.24,0.41],[0.01,0.03],[0.02,0.06]>
<b>C7</b>	<[0.20,0.36],[0.10,0.12],[0.09,0.12]>	<[0.22,0.39],[0.02,0.06],[0.03,0.08]>	<[0.22,0.39],[0.03,0.06],[0.03,0.09]>
<b>C8</b>	<[0.21,0.38],[0.03,0.07],[0.04,0.09]>	<[0.20,0.36],[0.10,0.11],[0.09,0.12]>	<[0.22,0.39],[0.03,0.06],[0.04,0.09]>
<b>C9</b>	<[0.21,0.38],[0.04,0.08],[0.04,0.10]>	<[0.21,0.38],[0.03,0.07],[0.04,0.10]>	<[0.20,0.36],[0.10,0.12],[0.09,0.13]>
<b>C10</b>	<[0.19,0.35],[0.05,0.09],[0.05,0.11]>	<[0.20,0.35],[0.05,0.09],[0.05,0.11]>	<[0.20,0.36],[0.04,0.08],[0.05,0.10]>
<b>C11</b>	<[0.20,0.36],[0.04,0.08],[0.05,0.10]>	<[0.20,0.36],[0.05,0.09],[0.05,0.11]>	<[0.20,0.36],[0.04,0.08],[0.05,0.10]>
<b>C12</b>	<[0.18,0.33],[0.06,0.11],[0.07,0.13]>	<[0.18,0.34],[0.06,0.11],[0.07,0.13]>	<[0.19,0.34],[0.05,0.10],[0.06,0.12]>
<b>C13</b>	<[0.18,0.33],[0.07,0.12],[0.08,0.14]>	<[0.18,0.33],[0.07,0.12],[0.07,0.14]>	<[0.18,0.34],[0.05,0.10],[0.06,0.12]>
<b>C14</b>	<[0.17,0.32],[0.07,0.12],[0.07,0.14]>	<[0.18,0.32],[0.06,0.12],[0.07,0.14]>	<[0.17,0.32],[0.07,0.12],[0.07,0.14]>
<b>C15</b>	<[0.17,0.31],[0.07,0.13],[0.07,0.14]>	<[0.17,0.31],[0.07,0.12],[0.07,0.14]>	<[0.17,0.32],[0.07,0.13],[0.07,0.14]>

Table 5 :(continued)

	<b>C10</b>	<b>C11</b>	<b>C12</b>
<b>C1</b>	<[0.28,0.46],[0.00,0.00],[0.00,0.03]>	<[0.28,0.46],[0.00,0.00],[0.00,0.03]>	<[0.29,0.48],[0.00,0.00],[0.00,0.03]>
<b>C2</b>	<[0.28,0.46],[0.00,0.00],[0.00,0.03]>	<[0.27,0.46],[0.00,0.00],[0.00,0.03]>	<[0.29,0.48],[0.00,0.00],[0.00,0.03]>
<b>C3</b>	<[0.27,0.45],[0.00,0.00],[0.00,0.04]>	<[0.27,0.45],[0.00,0.01],[0.01,0.04]>	<[0.28,0.47],[0.00,0.00],[0.00,0.03]>
<b>C4</b>	<[0.26,0.44],[0.00,0.00],[0.00,0.04]>	<[0.26,0.44],[0.00,0.01],[0.00,0.04]>	<[0.28,0.46],[0.00,0.00],[0.00,0.03]>
<b>C5</b>	<[0.26,0.43],[0.00,0.02],[0.01,0.05]>	<[0.26,0.43],[0.00,0.02],[0.01,0.05]>	<[0.27,0.46],[0.00,0.00],[0.00,0.04]>
<b>C6</b>	<[0.26,0.44],[0.00,0.00],[0.00,0.04]>	<[0.26,0.44],[0.00,0.00],[0.00,0.04]>	<[0.28,0.46],[0.00,0.00],[0.00,0.03]>
<b>C7</b>	<[0.23,0.41],[0.01,0.03],[0.02,0.07]>	<[0.23,0.41],[0.02,0.05],[0.03,0.07]>	<[0.25,0.43],[0.00,0.02],[0.01,0.05]>
<b>C8</b>	<[0.23,0.41],[0.01,0.03],[0.02,0.07]>	<[0.23,0.41],[0.01,0.03],[0.02,0.07]>	<[0.25,0.43],[0.00,0.01],[0.01,0.05]>
<b>C9</b>	<[0.23,0.40],[0.02,0.05],[0.03,0.08]>	<[0.23,0.40],[0.02,0.05],[0.03,0.08]>	<[0.24,0.42],[0.01,0.03],[0.02,0.06]>
<b>C10</b>	<[0.20,0.36],[0.10,0.11],[0.08,0.12]>	<[0.21,0.38],[0.02,0.06],[0.03,0.08]>	<[0.23,0.40],[0.01,0.03],[0.02,0.07]>
<b>C11</b>	<[0.21,0.38],[0.03,0.06],[0.04,0.09]>	<[0.20,0.36],[0.10,0.11],[0.08,0.12]>	<[0.23,0.40],[0.01,0.03],[0.02,0.07]>

<b>C1</b> <b>2</b>	<[0.20,0.36],[0.05,0.08],[0.05,0.10]>	<[0.20,0.36],[0.05,0.08],[0.05,0.11]>	<[0.20,0.36],[0.10,0.10],[0.08,0.12]>
<b>C1</b> <b>3</b>	<[0.20,0.36],[0.05,0.08],[0.05,0.11]>	<[0.20,0.35],[0.05,0.08],[0.05,0.11]>	<[0.21,0.37],[0.03,0.06],[0.04,0.09]>
<b>C1</b> <b>4</b>	<[0.19,0.34],[0.06,0.10],[0.06,0.12]>	<[0.19,0.34],[0.06,0.10],[0.06,0.12]>	<[0.20,0.36],[0.04,0.07],[0.05,0.10]>
<b>C1</b> <b>5</b>	<[0.18,0.33],[0.06,0.10],[0.06,0.12]>	<[0.18,0.33],[0.06,0.10],[0.06,0.12]>	<[0.19,0.35],[0.05,0.08],[0.05,0.10]>

Table 5 :(continued)

	<b>C13</b>	<b>C14</b>	<b>C15</b>
<b>C1</b>	<[0.29,0.48],[0.00,0.00],[0.00,0.03]>	<[0.31,0.49],[0.00,0.00],[0.00,0.01]>	<[0.31,0.50],[0.00,0.00],[0.00,0.01]>
<b>C2</b>	<[0.29,0.48],[0.00,0.00],[0.00,0.03]>	<[0.30,0.49],[0.00,0.00],[0.00,0.01]>	<[0.31,0.50],[0.00,0.00],[0.00,0.01]>
<b>C3</b>	<[0.28,0.47],[0.00,0.00],[0.00,0.03]>	<[0.30,0.48],[0.00,0.00],[0.00,0.01]>	<[0.31,0.49],[0.00,0.00],[0.00,0.01]>
<b>C4</b>	<[0.28,0.47],[0.00,0.00],[0.00,0.03]>	<[0.29,0.47],[0.00,0.00],[0.00,0.01]>	<[0.30,0.48],[0.00,0.00],[0.00,0.01]>
<b>C5</b>	<[0.27,0.45],[0.00,0.01],[0.01,0.04]>	<[0.28,0.46],[0.00,0.01],[0.01,0.04]>	<[0.29,0.47],[0.00,0.00],[0.00,0.01]>
<b>C6</b>	<[0.28,0.46],[0.00,0.00],[0.00,0.03]>	<[0.29,0.47],[0.00,0.00],[0.00,0.01]>	<[0.30,0.48],[0.00,0.00],[0.00,0.01]>
<b>C7</b>	<[0.26,0.44],[0.00,0.01],[0.00,0.04]>	<[0.26,0.44],[0.00,0.01],[0.01,0.04]>	<[0.27,0.45],[0.00,0.01],[0.01,0.04]>
<b>C8</b>	<[0.26,0.43],[0.00,0.01],[0.00,0.04]>	<[0.26,0.44],[0.00,0.01],[0.01,0.04]>	<[0.27,0.44],[0.00,0.01],[0.01,0.04]>
<b>C9</b>	<[0.24,0.43],[0.01,0.03],[0.02,0.06]>	<[0.26,0.44],[0.00,0.02],[0.01,0.04]>	<[0.27,0.44],[0.00,0.01],[0.01,0.04]>
<b>C10</b>	<[0.23,0.40],[0.01,0.03],[0.02,0.07]>	<[0.25,0.41],[0.00,0.02],[0.01,0.04]>	<[0.25,0.42],[0.00,0.01],[0.01,0.04]>
<b>C11</b>	<[0.23,0.40],[0.01,0.03],[0.02,0.07]>	<[0.25,0.41],[0.00,0.02],[0.01,0.04]>	<[0.25,0.42],[0.00,0.01],[0.01,0.04]>
<b>C12</b>	<[0.22,0.38],[0.02,0.05],[0.03,0.08]>	<[0.23,0.39],[0.01,0.03],[0.02,0.06]>	<[0.23,0.40],[0.01,0.03],[0.02,0.05]>
<b>C13</b>	<[0.20,0.35],[0.10,0.10],[0.08,0.12]>	<[0.23,0.39],[0.01,0.03],[0.02,0.06]>	<[0.23,0.40],[0.01,0.03],[0.02,0.05]>
<b>C14</b>	<[0.20,0.36],[0.04,0.07],[0.05,0.10]>	<[0.20,0.35],[0.09,0.10],[0.08,0.10]>	<[0.23,0.39],[0.00,0.02],[0.01,0.05]>
<b>C15</b>	<[0.19,0.35],[0.05,0.08],[0.05,0.10]>	<[0.20,0.35],[0.05,0.08],[0.05,0.09]>	<[0.20,0.34],[0.09,0.10],[0.08,0.10]>

**Step 4 :** Obtaining the sum of rows and columns using the predefined formula (3) and (4) . The sum of rows is denoted by (D), and the sum of columns is denoted by (R).

**Step 5 :** Calculate the weights of attributes by using the formula (6) , as presented in Table 7 and Figure .19.

$$W_i = \frac{\sqrt{((S(D_i+R_i))^2 + (S(D_i-R_i))^2)}}{\sum_{i=1}^n \sqrt{((S(D_i+R_i))^2 + (S(D_i-R_i))^2)}} \quad i = 1,2,3, \dots \dots n \tag{6}$$

Table 6: The relative weights for each criterion using N-DEMATEL technique

<b>Criteria</b>	<b>Weights</b>
-----------------	----------------

C15	0.06728011
C1	0.067037378
C2	0.066978636
C14	0.06695252
C13	0.066892234
C12	0.066809228
C3	0.066754041
C4	0.066496641
C5	0.066489133
C11	0.066444645
C10	0.066417786
C6	0.066384715
C8	0.06637841
C9	0.066355817
C7	0.066328707

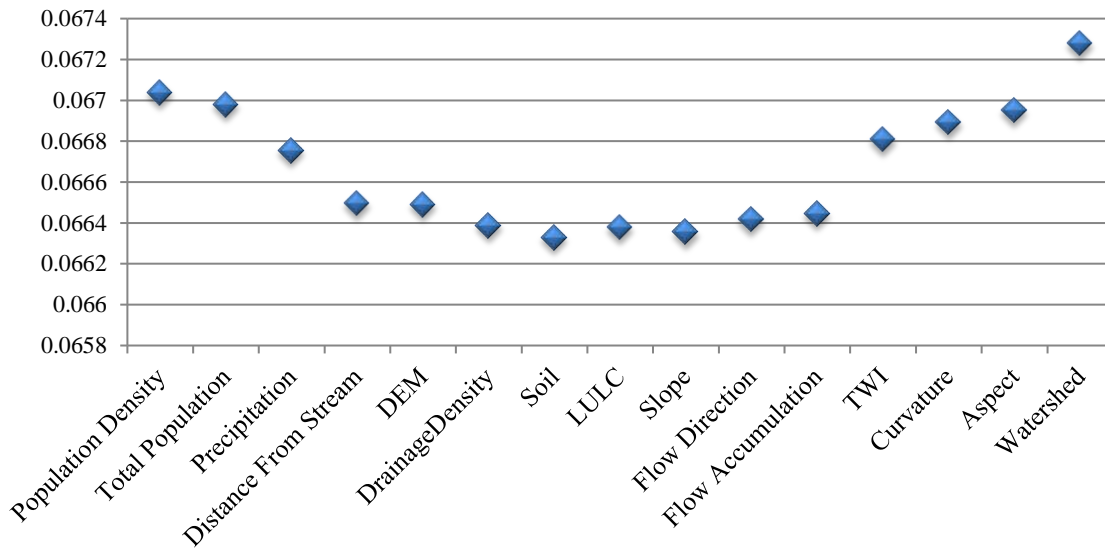


Figure 19: Weights of flash floods controlling factors

## 6. RESULTS AND DISCUSSION

The applications of a multi-criteria decision-making analysis in our study area were used for evaluating the relative weights of flood controlling factor. The weights of the flood variables were calculated using N-DEMATEL model through evaluating criteria based on their expected significances. The integration of GIS-environment with N-DEMATEL technique provides more flexibility to assess the causative agents of flooding.

We identified flood influencing factors and by using these factors in multi-criteria analysis we developed a flood susceptibility map of the study area. Regarding our flood influencing factors, the elevation factor was within the range from 17 m to 879 m . The slope factor was within the range from 0° to 66.6° .The topographic wetness index was within the range from 2.6648 to 26.3782. The aspect factor was grouped into ten classes : [ Flat (-1) , North (0-22.5)

, Northeast (22.5-67.5) , East (67.5-112.5) , Southeast (112.5-157.5) , South (157.5-202.5) , Southwest (202.5-247.5) , West (247.5-292.5), Northwest (292.5-337.5) and North (337.5-360)) . The hydrological parameters for the study area including flow direction, flow Accumulation, watersheds and drainage density can be seen in Figure 7 , Figure 8 , Figure 13 and Figure 16 . The soil factor was grouped into four classes: ( Gravels and gravelly sand soil , Water , stony soils and Nile alluvium) . The LULC factor was grouped into four classes: ( Stony\_Area , Bare\_Soil, Vegetation and Urban) . The precipitation factor was within the range from 2.8 mm to 16.3327 mm. The curvature factor was within the range from -14.92 to 12.7. The distance from streams factor was within the range from 0 m to 2696.4 m. By using the N- DEMATEL multi-criteria analysis method, the weight of each factor calculated and obtained the following results: 0.067037378 for Population Density, 0.066978636 for Total Population, 0.066754041 for Precipitation, 0.066496641 for Distance From Stream, 0.066489133 for Elevation, 0.066384715 for Drainage Density, 0.066328707 for Soil, 0.06637841 for (LULC), 0.066355817 for (Slope), 0.066417786 for Flow Direction, 0.066444645 for Flow Accumulation, 0.066809228 for TWI, 0.066892234 for Curvature, 0.06695252 for Aspect and 0.06728011 for Watershed. Flood hazard map and was generated using the following equation:

$$FHM = \sum (C1Wj1 + C2Wj2 + C3Wj3 + CnWjn),$$

Where,  $Wj$  is the weight of each factor;  $n$  is the number of factors,  $C1, C2, C3,$  and  $Cn$  are the respective factors. In our study, five classes were identified: very high, high, moderate, low, and very low.

The resulting hazard map shows that Manfalut , Asyut and Al-Qusiyyah are the most vulnerable to flooding, while Al-Ghanayim, Asyut1, Asyut2 and New Asyut are the least vulnerable to flooding. as seen in Figure .20, Figure .21 and Figure .21.

Our results reveal that ‘very high’ susceptibility category reflects approximately 5 %. Whilst the ‘high’ susceptibility class reflects approximately 12% and the ‘moderate’ susceptibility category covers approximately 26%. Furthermore, the ‘low’ susceptibility category reflects approximately 35% and the ‘very low’ susceptibility class reflects approximately 22% of our study area.

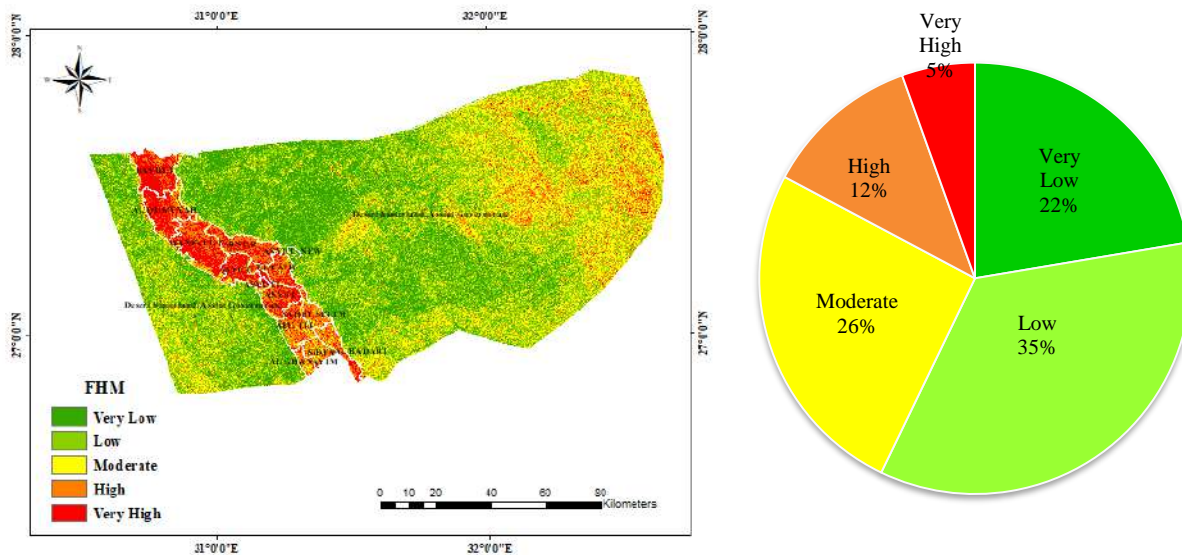


Figure 20: Susceptibility map

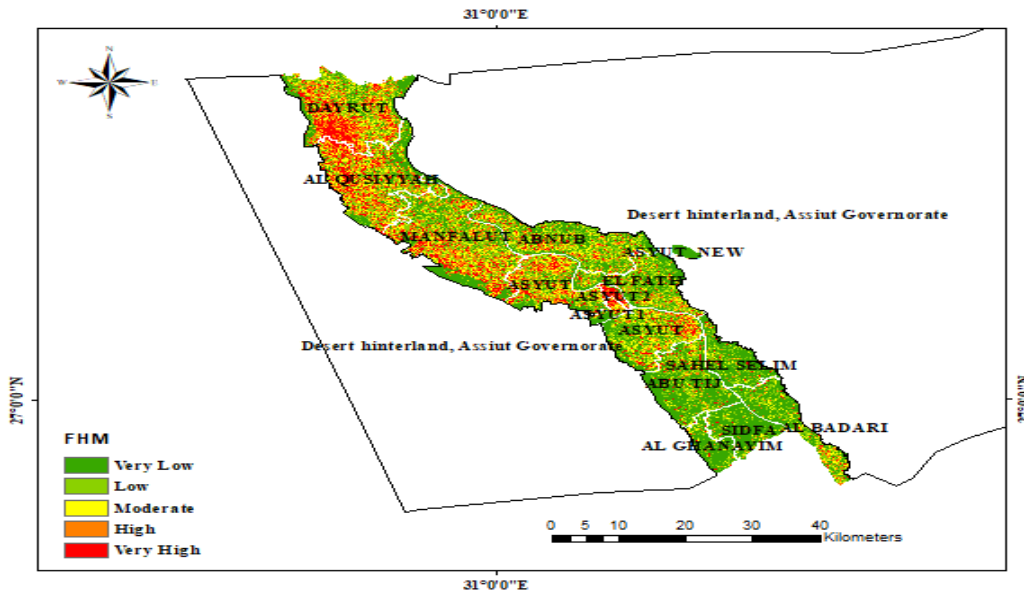


Figure 21: Flood hazard map

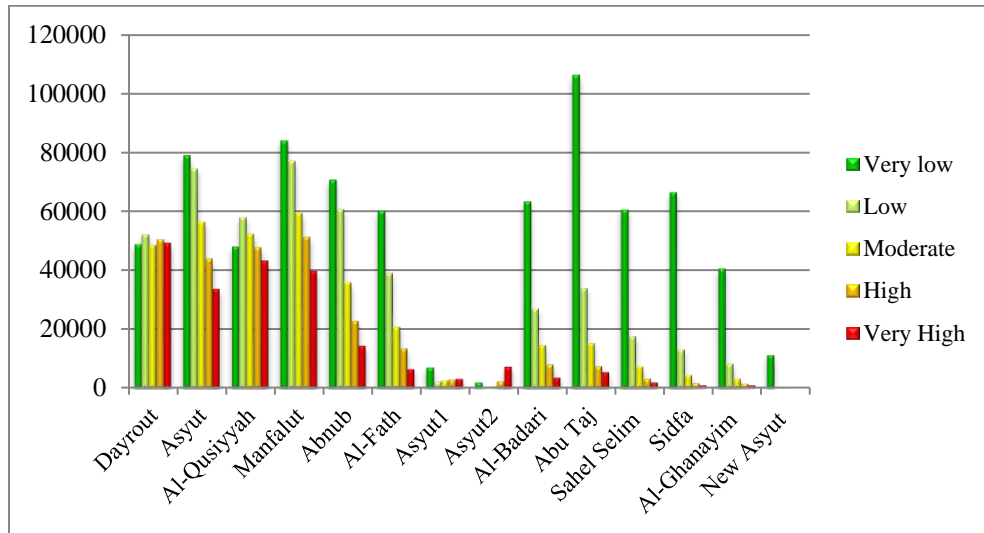


Figure 22: Vulnerability Percentages in Asyut's urban districts

### 7. Concluding Remarks

Flood susceptibility map provides valuable data for decision-makers and the planners dealing with flood hazards and susceptibility. Flood susceptibility map provides residents with information about probable damage and how to prevent potential disasters. Our study area is in Upper Egypt in the Asyut governorate. To analyze the influence of flash floods on study area, fifteen influencing factors such as elevation, slope, topographic wetness index, distance from the stream, flow accumulation, aspect, flow direction, soil, land cover, watershed, curvature, drainage density, total population, population density and precipitation were determined. The weight of each factor calculated by using the N-DEMATEL multi criteria analysis method and obtained the following results: 0.067037378 for Population Density, 0.066978636 for Total Population, 0.066754041 for Precipitation, 0.066496641 for Distance From Stream, 0.066489133 for Elevation, 0.066384715 for Drainage Density, 0.066328707 for Soil, 0.06637841 for (LULC), 0.066355817 for (Slope), 0.066417786 for Flow Direction, 0.066444645 for Flow Accumulation, 0.066809228 for TWI, 0.066892234 for Curvature, 0.06695252 for Aspect and 0.06728011 for Watershed. Our

results reveal that ‘very high’ susceptibility category reflects approximately 5 %. whilst the ‘high’ susceptibility class reflects approximately 12% and the ‘moderate’ susceptibility category covers approximately 26%. Furthermore, the ‘low’ susceptibility category reflects approximately 35% and the ‘very low’ susceptibility class reflects approximately 22% of our study area. From our study, we concluded that the integration of remotely sensed data and geographical information system (GIS) with neutrosophic DEMATEL is a valuable and an appropriate tool to assess flash flood susceptibility.

In the future, we will analyze the influence of flash floods on various study areas using various neutrosophic MCDM techniques and geographical information system.

**Limitation of Proposed Research:** More involvements from more companies will make our research better.

### Competing Interests

The authors announce that there is no discrepancy of interest concerning the publication of this research.

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**Appendix A** : Normalize the direct-relation decision matrix

Normalize the direct-relation decision matrix T lower

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15
C1	0.03 6	0.05 4	0.05 4	0.05 7	0.05 7	0.05 7	0.06 8	0.06 4	0.05 7	0.06 8	0.06 8	0.06 8	0.06 8	0.07 1	0.07 1
C2	0.05 0	0.03 6	0.05 4	0.05 7	0.05 7	0.05 7	0.06 8	0.06 4	0.05 7	0.06 8	0.06 8	0.06 8	0.06 8	0.07 1	0.07 1
C3	0.05 0	0.05 0	0.03 6	0.06 4	0.05 7	0.05 4	0.05 7	0.05 7	0.05 4	0.06 8	0.06 4	0.06 8	0.06 8	0.07 1	0.07 1
C4	0.04 6	0.04 6	0.04 3	0.03 6	0.05 4	0.05 7	0.05 4	0.06 4	0.05 7	0.06 8	0.06 8	0.06 8	0.06 8	0.07 1	0.07 1
C5	0.04 6	0.04 6	0.04 6	0.05 0	0.03 6	0.05 7	0.05 4	0.05 7	0.05 7	0.06 4	0.06 4	0.06 8	0.06 4	0.06 4	0.07 1
C6	0.04 6	0.04 6	0.05 0	0.04 6	0.04 6	0.03 6	0.05 7	0.06 4	0.05 7	0.06 8	0.06 8	0.06 8	0.06 8	0.07 1	0.07 1
C7	0.03 9	0.03 9	0.04 6	0.05 0	0.05 0	0.04 6	0.03 6	0.05 4	0.05 4	0.05 7	0.05 4	0.06 4	0.06 8	0.06 4	0.06 4
C8	0.04 3	0.04 3	0.04 6	0.04 3	0.04 6	0.04 3	0.05 0	0.03 6	0.05 4	0.05 7	0.05 7	0.06 4	0.06 8	0.06 4	0.06 4
C9	0.04 6	0.04 6	0.05 0	0.04 6	0.04 6	0.04 6	0.05 0	0.05 0	0.03 6	0.05 4	0.05 4	0.05 7	0.05 7	0.06 4	0.06 4
C10	0.03 0	0.03 9	0.03 9	0.03 9	0.04 3	0.03 9	0.04 6	0.04 6	0.05 0	0.03 6	0.05 4	0.05 7	0.05 7	0.06 4	0.06 4
C11	0.03 1	0.03 9	0.04 3	0.03 9	0.04 3	0.03 9	0.05 0	0.04 6	0.05 0	0.05 0	0.03 6	0.05 7	0.05 7	0.06 4	0.06 4
C12	0.03 2	0.03 9	0.03 9	0.03 9	0.03 9	0.03 9	0.04 3	0.04 3	0.04 6	0.04 6	0.04 6	0.03 6	0.05 4	0.05 7	0.05 7
C13	0.03 3	0.03 9	0.03 9	0.03 9	0.04 3	0.03 9	0.03 9	0.03 9	0.04 6	0.04 6	0.04 6	0.05 0	0.03 6	0.05 7	0.05 7
C14	0.03 4	0.03 6	0.03 6	0.03 6	0.04 3	0.03 6	0.04 3	0.04 3	0.04 3	0.04 3	0.04 3	0.04 6	0.04 6	0.03 6	0.06 4
C15	0.03 5	0.03 6	0.03 6	0.03 6	0.03 6	0.03 6	0.04 3	0.04 3	0.04 3	0.04 3	0.04 3	0.04 6	0.04 6	0.04 3	0.03 6

Normalize the direct-relation decision matrix T upper

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15
C1	0.03 6	0.06 1	0.06 1	0.06 4	0.06 4	0.06 4	0.07 1	0.06 8	0.06 4	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1
C2	0.05 7	0.03 6	0.06 1	0.06 4	0.06 4	0.06 4	0.07 1	0.06 8	0.06 4	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1
C3	0.05 7	0.05 7	0.03 6	0.06 8	0.06 4	0.06 1	0.06 4	0.06 4	0.06 1	0.07 1	0.06 8	0.07 1	0.07 1	0.07 1	0.07 1
C4	0.05 4	0.05 4	0.05 0	0.03 6	0.06 1	0.06 4	0.06 1	0.06 8	0.06 4	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1
C5	0.05 4	0.05 4	0.05 4	0.05 7	0.03 6	0.06 4	0.06 1	0.06 4	0.06 4	0.06 8	0.06 8	0.07 1	0.06 8	0.06 8	0.07 1

C6	0.05 4	0.05 4	0.05 7	0.05 4	0.05 4	0.03 6	0.06 4	0.06 8	0.06 4	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1	0.07 1
C7	0.04 6	0.04 6	0.05 4	0.05 7	0.05 7	0.05 4	0.03 6	0.06 1	0.06 1	0.06 4	0.06 1	0.06 8	0.07 1	0.06 8	0.06 8
C8	0.05 0	0.05 0	0.05 4	0.05 0	0.05 4	0.05 0	0.05 7	0.03 6	0.06 1	0.06 4	0.06 4	0.06 8	0.07 1	0.06 8	0.06 8
C9	0.05 4	0.05 4	0.05 7	0.05 4	0.05 4	0.05 4	0.05 7	0.05 7	0.03 6	0.06 1	0.06 1	0.06 4	0.06 4	0.06 8	0.06 8
C1 0	0.04 6	0.04 6	0.04 6	0.04 6	0.05 0	0.04 6	0.05 4	0.05 4	0.05 7	0.03 6	0.06 1	0.06 4	0.06 4	0.06 8	0.06 8
C1 1	0.04 6	0.04 6	0.05 0	0.04 6	0.05 0	0.04 6	0.05 7	0.05 4	0.05 7	0.05 7	0.03 6	0.06 4	0.06 4	0.06 8	0.06 8
C1 2	0.04 6	0.04 6	0.04 6	0.04 6	0.04 6	0.04 6	0.05 0	0.05 0	0.05 4	0.05 4	0.05 4	0.03 6	0.06 1	0.06 4	0.06 4
C1 3	0.04 6	0.04 6	0.04 6	0.04 6	0.05 0	0.04 6	0.04 6	0.04 6	0.05 4	0.05 4	0.05 4	0.05 7	0.03 6	0.06 4	0.06 4
C1 4	0.04 3	0.04 3	0.04 3	0.04 3	0.05 0	0.04 3	0.05 0	0.05 0	0.05 0	0.05 0	0.05 0	0.05 4	0.05 4	0.03 6	0.06 8
C1 5	0.04 3	0.04 3	0.04 3	0.04 3	0.04 3	0.04 3	0.05 0	0.05 0	0.05 0	0.05 0	0.05 0	0.05 4	0.05 4	0.05 0	0.03 6

Normalize the direct-relation decision matrix I lower

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15
C1	0.08 5	0.01 7	0.01 7	0.00 8	0.00 8	0.00 8	0.00 0	0.00 0	0.00 8	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C2	0.02 5	0.08 5	0.01 7	0.00 8	0.00 8	0.00 8	0.00 0	0.00 0	0.00 8	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C3	0.02 5	0.02 5	0.08 5	0.00 0	0.00 8	0.01 7	0.00 8	0.00 8	0.01 7	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C4	0.03 4	0.03 4	0.04 2	0.08 5	0.01 7	0.00 8	0.01 7	0.00 0	0.00 8	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C5	0.03 4	0.03 4	0.03 4	0.02 5	0.08 5	0.00 8	0.01 7	0.00 8	0.00 8	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C6	0.03 4	0.03 4	0.02 5	0.03 4	0.03 4	0.08 5	0.00 8	0.00 0	0.00 8	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C7	0.05 1	0.05 1	0.03 4	0.02 5	0.02 5	0.03 4	0.08 5	0.01 7	0.01 7	0.00 8	0.01 7	0.00 0	0.00 0	0.00 0	0.00 0
C8	0.04 2	0.04 2	0.03 4	0.04 2	0.03 4	0.04 2	0.02 5	0.08 5	0.01 7	0.00 8	0.00 8	0.00 0	0.00 0	0.00 0	0.00 0
C9	0.03 4	0.03 4	0.02 5	0.03 4	0.03 4	0.03 4	0.02 5	0.02 5	0.08 5	0.01 7	0.01 7	0.00 8	0.00 8	0.00 0	0.00 0
C1 0	0.05 1	0.05 1	0.05 1	0.05 1	0.04 2	0.05 1	0.03 4	0.03 4	0.02 5	0.08 5	0.01 7	0.00 8	0.00 8	0.00 0	0.00 0
C1 1	0.05 1	0.05 1	0.04 2	0.05 1	0.04 2	0.05 1	0.02 5	0.03 4	0.02 5	0.02 5	0.08 5	0.00 8	0.00 8	0.00 0	0.00 0
C1 2	0.05 1	0.05 1	0.05 1	0.05 1	0.05 1	0.05 1	0.04 2	0.04 2	0.03 4	0.03 4	0.03 4	0.08 5	0.01 7	0.00 8	0.00 8
C1 3	0.05 1	0.05 1	0.05 1	0.05 1	0.04 2	0.05 1	0.05 1	0.05 1	0.03 4	0.03 4	0.03 4	0.02 5	0.08 5	0.00 8	0.00 8

C1	0.05	0.05	0.05	0.05	0.04	0.05	0.04	0.04	0.04	0.04	0.04	0.03	0.03	0.08	0.00
4	9	9	9	9	2	9	2	2	2	2	2	4	4	5	0
C1	0.05	0.05	0.05	0.05	0.05	0.05	0.04	0.04	0.04	0.04	0.04	0.03	0.03	0.04	0.08
5	9	9	9	9	9	9	2	2	2	2	2	4	4	2	5

Normalize the direct-relation decision matrix I upper

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15
C1	0.08	0.03	0.03	0.01	0.01	0.01	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00
	5	4	4	7	7	7	0	8	7	0	0	0	0	0	0
C2	0.04	0.08	0.03	0.01	0.01	0.01	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00
	2	5	4	7	7	7	0	8	7	0	0	0	0	0	0
C3	0.04	0.04	0.08	0.00	0.01	0.03	0.01	0.01	0.03	0.00	0.00	0.00	0.00	0.00	0.00
	2	2	5	8	7	4	7	7	4	0	8	0	0	0	0
C4	0.05	0.05	0.05	0.08	0.03	0.01	0.03	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00
	1	1	9	5	4	7	4	8	7	0	0	0	0	0	0
C5	0.05	0.05	0.05	0.04	0.08	0.01	0.03	0.01	0.01	0.00	0.00	0.00	0.00	0.00	0.00
	1	1	1	2	5	7	4	7	7	8	8	0	8	8	0
C6	0.05	0.05	0.04	0.05	0.05	0.08	0.01	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00
	1	1	2	1	1	5	7	8	7	0	0	0	0	0	0
C7	0.06	0.06	0.05	0.04	0.04	0.05	0.08	0.03	0.03	0.01	0.03	0.00	0.00	0.00	0.00
	8	8	1	2	2	1	5	4	4	7	4	8	0	8	8
C8	0.05	0.05	0.05	0.05	0.05	0.05	0.04	0.08	0.03	0.01	0.01	0.00	0.00	0.00	0.00
	9	9	1	9	1	9	2	5	4	7	7	8	0	8	8
C9	0.05	0.05	0.04	0.05	0.05	0.05	0.04	0.04	0.08	0.03	0.03	0.01	0.01	0.00	0.00
	1	1	2	1	1	1	2	2	5	4	4	7	7	8	8
C1	0.06	0.06	0.06	0.06	0.05	0.06	0.05	0.05	0.04	0.08	0.03	0.01	0.01	0.00	0.00
	0	8	8	8	9	8	1	1	2	5	4	7	7	8	8
C1	0.06	0.06	0.05	0.06	0.05	0.06	0.04	0.05	0.04	0.04	0.08	0.01	0.01	0.00	0.00
	1	8	8	9	8	9	8	2	1	2	2	5	7	7	8
C1	0.06	0.06	0.06	0.06	0.06	0.06	0.05	0.05	0.05	0.05	0.05	0.08	0.03	0.01	0.01
	2	8	8	8	8	8	9	9	1	1	1	5	4	7	7
C1	0.06	0.06	0.06	0.06	0.05	0.06	0.06	0.06	0.05	0.05	0.05	0.05	0.04	0.08	0.01
	3	8	8	8	9	8	8	8	1	1	1	2	5	7	7
C1	0.07	0.07	0.07	0.07	0.05	0.07	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.08	0.00
	4	6	6	6	9	6	9	9	9	9	9	1	1	5	8
C1	0.07	0.07	0.07	0.07	0.07	0.07	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.08
	5	6	6	6	6	6	9	9	9	9	9	1	1	9	5

Normalize the direct-relation decision matrix F lower

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15
C1	0.07	0.02	0.02	0.01	0.01	0.01	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00
	1	1	1	4	4	4	0	7	4	0	0	0	0	0	0
C2	0.02	0.07	0.02	0.01	0.01	0.01	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00
	9	1	1	4	4	4	0	7	4	0	0	0	0	0	0

C3	0.02 9	0.02 9	0.07 1	0.00 7	0.01 4	0.02 1	0.01 4	0.01 4	0.02 1	0.00 0	0.00 7	0.00 0	0.00 0	0.00 0	0.00 0
C4	0.03 6	0.03 6	0.04 3	0.07 1	0.02 1	0.01 4	0.02 1	0.00 7	0.01 4	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C5	0.03 6	0.03 6	0.03 6	0.02 9	0.07 1	0.01 4	0.02 1	0.01 4	0.01 4	0.00 7	0.00 7	0.00 0	0.00 7	0.00 7	0.00 0
C6	0.03 6	0.03 6	0.02 9	0.03 6	0.03 6	0.07 1	0.01 4	0.00 7	0.01 4	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0	0.00 0
C7	0.05 0	0.05 0	0.03 6	0.02 9	0.02 9	0.03 6	0.07 1	0.02 1	0.02 1	0.01 4	0.02 1	0.00 7	0.00 0	0.00 7	0.00 7
C8	0.04 3	0.04 3	0.03 6	0.04 3	0.03 6	0.04 3	0.02 9	0.07 1	0.02 1	0.01 4	0.01 4	0.00 7	0.00 0	0.00 7	0.00 7
C9	0.03 6	0.03 6	0.02 9	0.03 6	0.03 6	0.03 6	0.02 9	0.02 9	0.07 1	0.02 1	0.02 1	0.01 4	0.01 4	0.00 7	0.00 7
C1 0	0.05 0	0.05 0	0.05 0	0.05 0	0.04 3	0.05 0	0.03 6	0.03 6	0.02 9	0.07 1	0.02 1	0.01 4	0.01 4	0.00 7	0.00 7
C1 1	0.05 0	0.05 0	0.04 3	0.05 0	0.04 3	0.05 0	0.02 9	0.03 6	0.02 9	0.02 9	0.07 1	0.01 4	0.01 4	0.00 7	0.00 7
C1 2	0.05 0	0.05 0	0.05 0	0.05 0	0.05 0	0.05 0	0.04 3	0.04 3	0.03 6	0.03 6	0.03 6	0.07 1	0.02 1	0.01 4	0.01 4
C1 3	0.05 0	0.05 0	0.05 0	0.05 0	0.04 3	0.05 0	0.05 0	0.05 0	0.03 6	0.03 6	0.03 6	0.02 9	0.07 1	0.01 4	0.01 4
C1 4	0.05 7	0.05 7	0.05 7	0.05 7	0.04 3	0.05 7	0.04 3	0.04 3	0.04 3	0.04 3	0.04 3	0.03 6	0.03 6	0.07 1	0.01 7
C1 5	0.05 7	0.05 7	0.05 7	0.05 7	0.05 7	0.05 7	0.04 3	0.04 3	0.04 3	0.04 3	0.04 3	0.03 6	0.03 6	0.04 3	0.07 1

Normalize the direct-relation decision matrix F upper

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15
C1	0.07 1	0.03 6	0.03 6	0.02 9	0.02 9	0.02 9	0.01 4	0.02 1	0.02 9	0.01 4	0.01 4	0.01 4	0.01 4	0.00 0	0.00 0
C2	0.04 3	0.07 1	0.03 6	0.02 9	0.02 9	0.02 9	0.01 4	0.02 1	0.02 9	0.01 4	0.01 4	0.01 4	0.01 4	0.00 0	0.00 0
C3	0.04 3	0.04 3	0.07 1	0.02 1	0.02 9	0.03 6	0.02 9	0.02 9	0.03 6	0.01 4	0.02 1	0.01 4	0.01 4	0.00 0	0.00 0
C4	0.05 0	0.05 0	0.05 7	0.07 1	0.03 6	0.02 9	0.03 6	0.02 1	0.02 9	0.01 4	0.01 4	0.01 4	0.01 4	0.00 0	0.00 0
C5	0.05 0	0.05 0	0.05 0	0.04 3	0.07 1	0.02 9	0.03 6	0.02 9	0.02 9	0.02 1	0.02 1	0.01 4	0.02 1	0.02 1	0.00 0
C6	0.05 0	0.05 0	0.04 3	0.05 0	0.05 0	0.07 1	0.02 9	0.02 1	0.02 9	0.01 4	0.01 4	0.01 4	0.01 4	0.00 0	0.00 0
C7	0.06 4	0.06 4	0.05 0	0.04 3	0.04 3	0.05 0	0.07 1	0.03 6	0.03 6	0.02 9	0.03 6	0.02 1	0.01 4	0.02 1	0.02 1
C8	0.05 7	0.05 7	0.05 0	0.05 7	0.05 0	0.05 7	0.04 3	0.07 1	0.03 6	0.02 9	0.02 9	0.02 1	0.01 4	0.02 1	0.02 1
C9	0.05 0	0.05 0	0.04 3	0.05 0	0.05 0	0.05 0	0.04 3	0.04 3	0.07 1	0.03 6	0.03 6	0.02 9	0.02 9	0.02 1	0.02 1
C1 0	0.06 4	0.06 4	0.06 4	0.06 4	0.05 7	0.06 4	0.05 0	0.05 0	0.04 3	0.07 1	0.03 6	0.02 9	0.02 9	0.02 1	0.02 1
C1 1	0.06 4	0.06 4	0.05 7	0.06 4	0.05 7	0.06 4	0.04 3	0.05 0	0.04 3	0.04 3	0.07 1	0.02 9	0.02 9	0.02 1	0.02 1

<b>C1</b>	<b>0.06</b>	<b>0.06</b>	<b>0.06</b>	<b>0.06</b>	<b>0.06</b>	<b>0.06</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.07</b>	<b>0.03</b>	<b>0.02</b>	<b>0.02</b>
<b>2</b>	<b>4</b>	<b>4</b>	<b>4</b>	<b>4</b>	<b>4</b>	<b>4</b>	<b>7</b>	<b>7</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>1</b>	<b>6</b>	<b>9</b>	<b>9</b>
<b>C1</b>	<b>0.06</b>	<b>0.06</b>	<b>0.06</b>	<b>0.06</b>	<b>0.05</b>	<b>0.06</b>	<b>0.06</b>	<b>0.06</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.04</b>	<b>0.07</b>	<b>0.02</b>	<b>0.02</b>
<b>3</b>	<b>4</b>	<b>4</b>	<b>4</b>	<b>4</b>	<b>7</b>	<b>4</b>	<b>4</b>	<b>4</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>3</b>	<b>1</b>	<b>9</b>	<b>9</b>
<b>C1</b>	<b>0.07</b>	<b>0.07</b>	<b>0.07</b>	<b>0.07</b>	<b>0.05</b>	<b>0.07</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.07</b>	<b>0.02</b>
<b>4</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>7</b>	<b>1</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>0</b>	<b>0</b>	<b>1</b>
<b>C1</b>	<b>0.07</b>	<b>0.07</b>	<b>0.07</b>	<b>0.07</b>	<b>0.07</b>	<b>0.07</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.05</b>	<b>0.07</b>
<b>5</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>7</b>	<b>0</b>	<b>0</b>	<b>7</b>